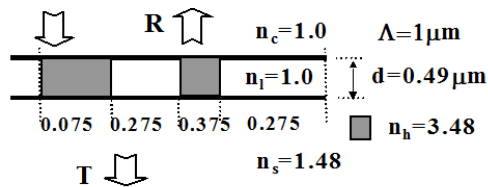
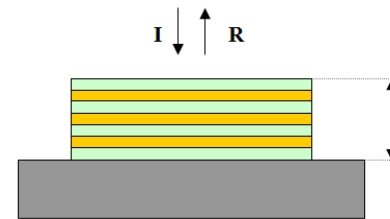
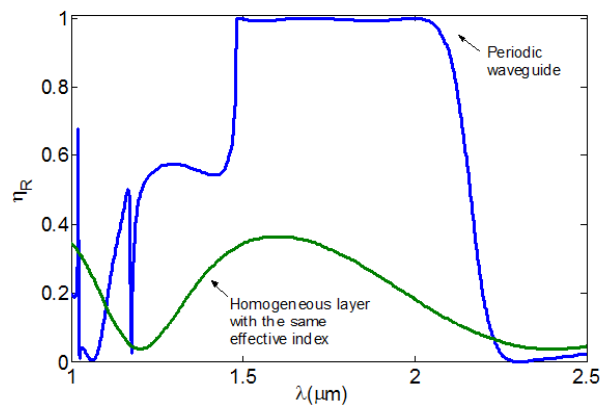


# Guided-mode resonance (GMR) effect for filtering devices in LCD display panels

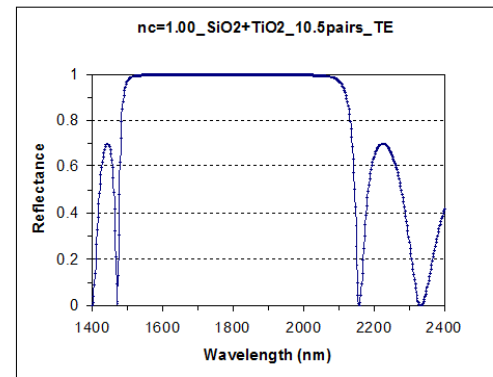
송 석 호, 한양대학교 물리학과, <http://optics.anyang.ac.kr/~shsong>



Single-layer SOI resonance device



21-layer SiO<sub>2</sub>/TiO<sub>2</sub> Bragg stack



Key  
notes

1. What is the GMR effect of waveguide gratings?
2. What is the photonic band structure (or, dispersion relation)?
3. What can we play with GMR filters for display?
4. What are the practical difficulties to be solved in GMR applications?

# Fabrication of Transmission Color Filters Using Silicon Subwavelength Gratings on Quartz Substrates

Yoshiaki Kanamori, Masaya Shimono, and Kazuhiro Hane Department of Nanomechanics, Tohoku University

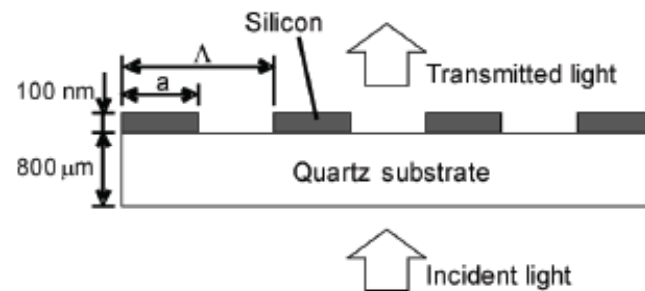


Fig. 1. Schematic of the fabricated color filter design. The grating period and width are defined as  $\Lambda$  and  $a$ , respectively.

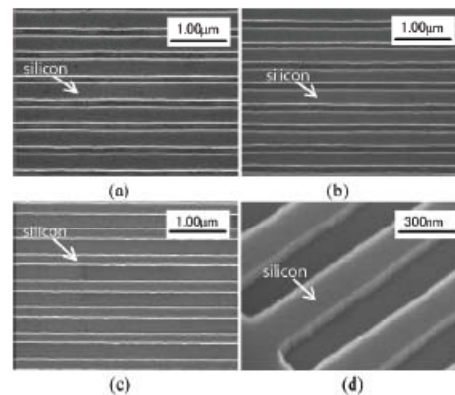


Fig. 2. SEM photographs of the fabricated gratings for (a) red ( $\Lambda = 400$  nm,  $a = 279$  nm), (b) green ( $\Lambda = 350$  nm,  $a = 231$  nm), and (c) blue ( $\Lambda = 440$  nm,  $a = 177$  nm) filters. (d) Oblique view of the fabricated grating for the blue filter at the edge.

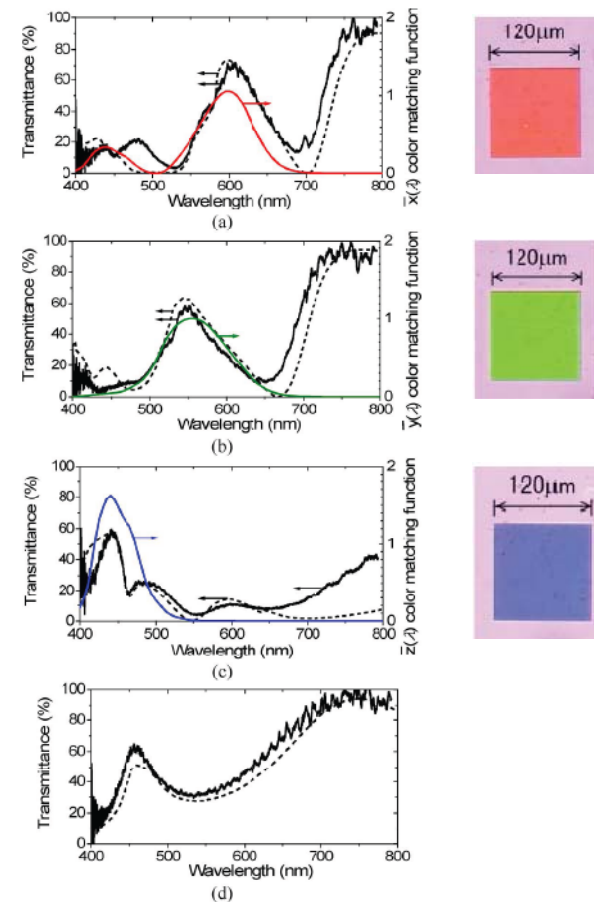


Fig. 4. Transmittances measured as a function of incident light wavelength for (a) red, (b) green, and (c) blue filters. (d) Transmittance of the bare SOQ substrate as a function of incident light wavelength. (Color version available online at <http://ieeexplore.ieee.org>.)

# 광파장 이하의 주기를 갖는 다결정 실리콘 격자 기반의 컬러필터

윤여택 · 이흥식 · 이상신<sup>†</sup>

광운대학교 전자공학과  
Ⓢ 139-701 서울특별시 노원구 월계동 447-1

김상훈 · 박주도 · 이기동

엘지전자기술원 소재재료연구소

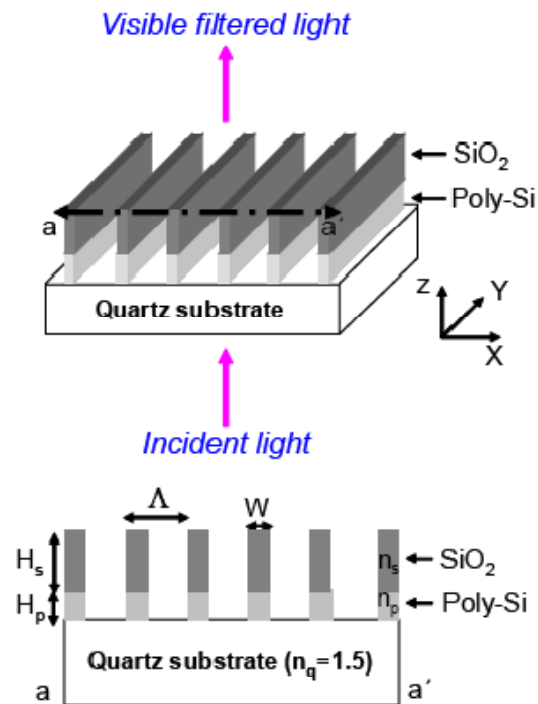
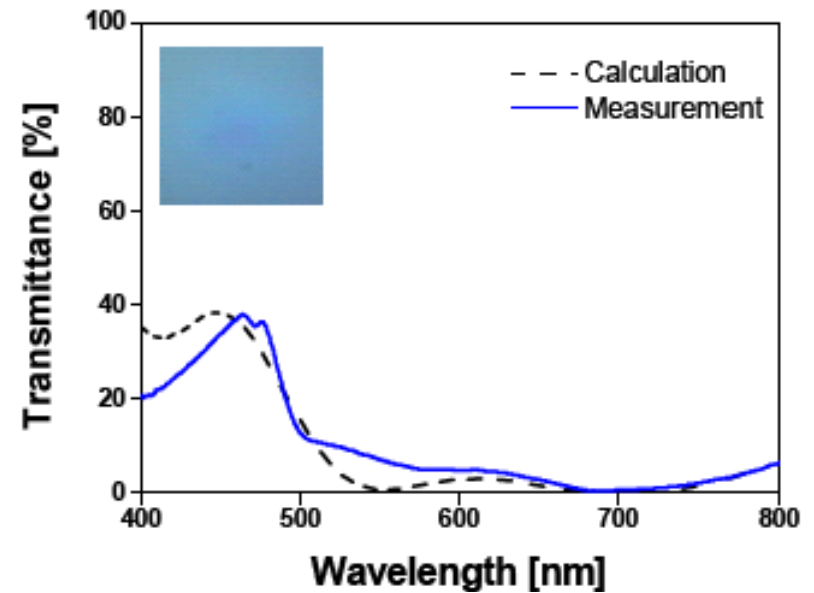
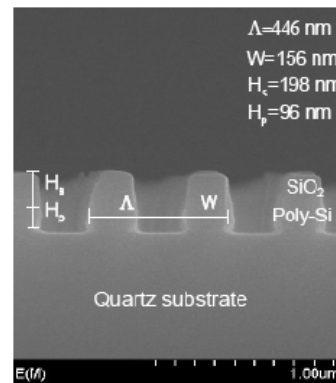


그림 1. 제안된 다결정 실리콘 컬러필터 구조.



## High angular tolerant color filter using subwavelength grating

Byoung-Ho Cheong,<sup>1</sup> O. N. Prudnikov,<sup>1</sup> Eunhyoung Cho,<sup>2</sup> Hae-Sung Kim,<sup>2</sup> Jaeho Yu,<sup>1</sup>  
Young-Sang Cho,<sup>1</sup> Hwan-Young Choi,<sup>1,a)</sup> and Sung Tae Shin<sup>1</sup>

<sup>1</sup>LCD R & D Center, Samsung Electronics Co., Nongseo-dong, Yongin-si, Gyeonggi-do 446-711,

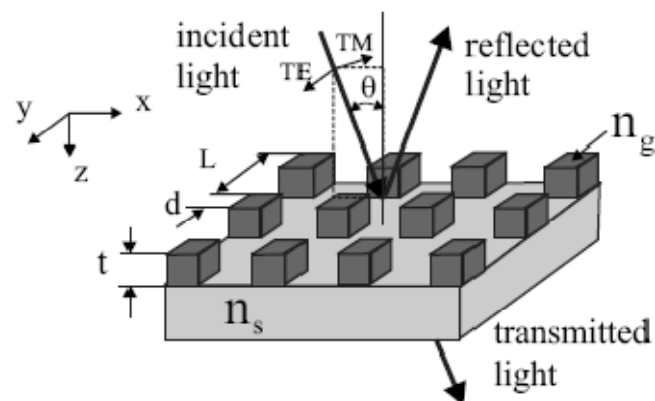


FIG. 1. Schematic geometry of subwavelength 2D grating structure.

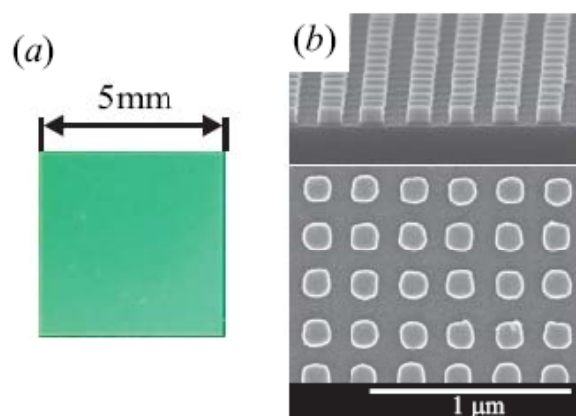


FIG. 4. (Color) (a) Photographic color image and (b) scanning electron microscope image of fabricated subwavelength grating slab.

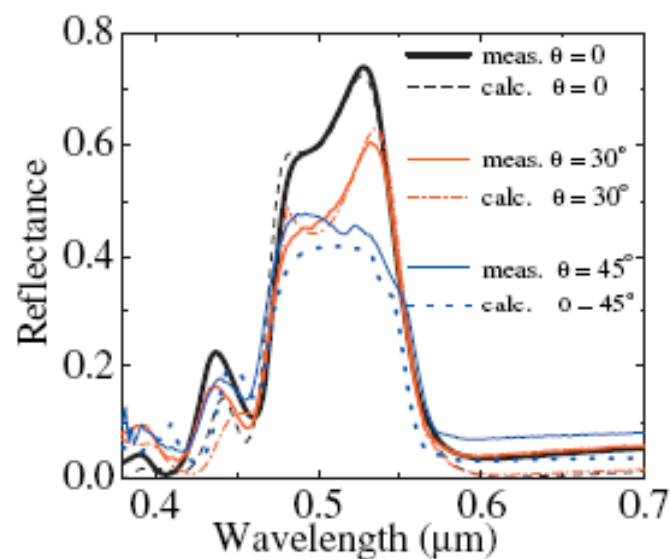


FIG. 5. (Color) Comparisons of measured and calculated reflectance curves with respect to different incident angles  $\theta$  (unpolarized light).

# Silicon-Layer Guided-Mode Resonance Polarizer With 40-nm Bandwidth

K. J. Lee, R. LaComb, B. Britton, M. Shokooh-Saremi, H. Silva, E. Donkor, Y. Ding, and R. Magnusson

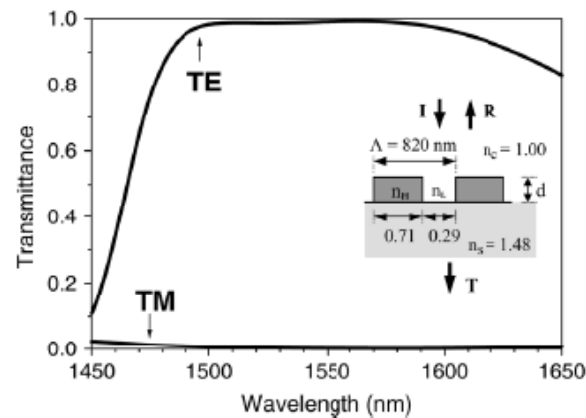


Fig. 2. Calculated spectral response of the designed GMR polarizer for TM- and TE-polarizations. The parameters are as follows: Thickness  $d = 500$  nm; refractive indices  $n_H = 3.48$ ,  $n_L = 1.00$ ,  $n_C = 1.00$ ,  $n_S = 1.48$ ; grating period  $\Lambda = 820$  nm; filling factor  $f = 0.71$ ; incident angle  $\theta_{\text{inc}} = 0^\circ$  (normal incidence).

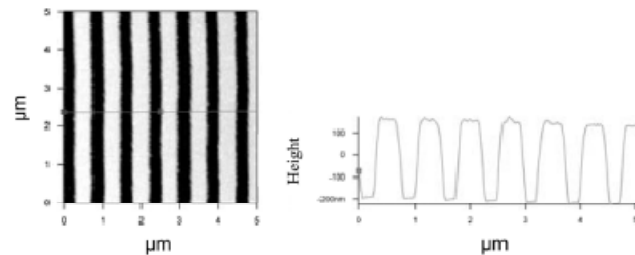


Fig. 4. AFM image of the polarizer and its profile quantifying the etch depth as 355 nm.

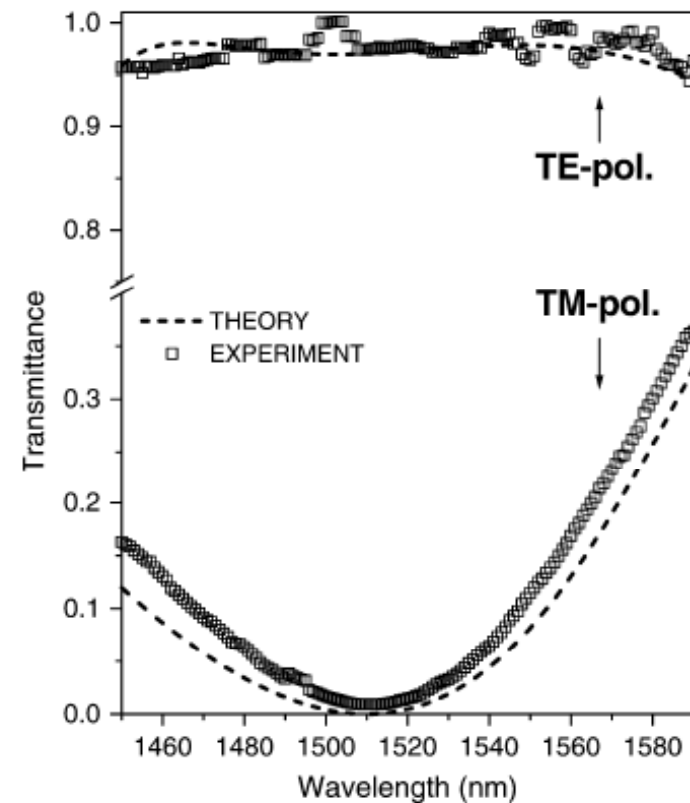
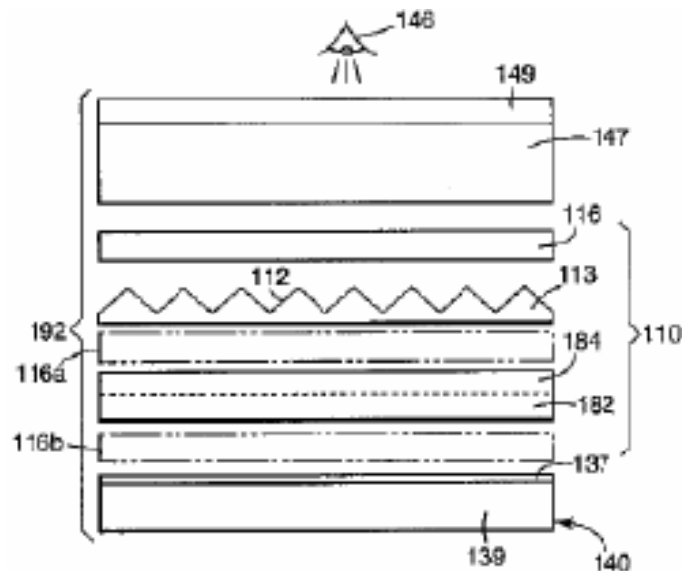


Fig. 5. Theoretical (dashed line) and experimental (hollow dot) spectral response of the fabricated GMR device for both TE- and TM-polarized incident waves. The experimental data is corrected for a  $\sim 4\%$  reflection at the backside of the substrate. Note that the vertical axis is divided.

# Reflective polarizer display, US 5828488 (1995.03.10), 3M (St. Paul, MN)

## DBEF와 편광필름의 투과도(532nm) (투과단위 :uW)



Input	5mW							
	DBEF(I)+532nm(I)		DBEF(-)+532nm(I)		DBEF(-)+532nm(-)		DBEF(I)+532nm(-)	
각도	투과	투과효율	투과	투과효율	투과	투과효율	투과	투과효율
0	4230	0.845	40	0.008	4420	0.884	130	0.026
5	4230	0.845	39	0.0078	4420	0.884	17	0.0034
10	4190	0.838	620	0.124	4350	0.87	13	0.0026
15	4190	0.838	47	0.0094	4420	0.884	425	0.085
20	4220	0.844	47	0.0094	4440	0.888	4.3	0.00088
25	4150	0.83	33	0.0066	4500	0.9	25	0.005
30	4090	0.818	27	0.0054	4400	0.88	46	0.0092
35	4030	0.806	95	0.019	4200	0.84	9.5	0.0019
40	3950	0.79	44	0.0088	4600	0.92	11.7	0.00234
45	3810	0.762	2.3	0.00046	4340	0.868	48	0.0096
50	3630	0.726	18	0.0036	4350	0.87	80	0.016
55	3400	0.68	26	0.0052	4300	0.86	27	0.0054
60	3140	0.628	8	0.0018	4550	0.91	60	0.012
65	2760	0.552	9	0.0018	4350	0.87	14	0.0028
70	2320	0.464	3.2	0.00064	2800	0.56	9.6	0.00192
75	1860	0.372	7	0.0014	2700	0.54	52	0.0104
80	1130	0.226	40	0.008	2100	0.42	29	0.0058
85	5050	1.01						

각도	편광필름(I)+532nm(I)		편광필름(-)+532nm(I)		편광필름(-)+532nm(-)		편광필름(I)+532nm(-)	
	투과	투과효율	투과	투과효율	투과	투과효율	투과	투과효율
0	3650	0.73	3.03	0.000606	3590	0.718	3	0.0006
5	3540	0.708	3.31	0.000662	3600	0.72	2.84	0.000568
10	3520	0.704	3.31	0.000662	3640	0.728	2.84	0.000568
15	3620	0.724	3.34	0.000668	3690	0.738	2.78	0.000556
20	3700	0.74	3.32	0.000664	3720	0.744	2.77	0.000554
25	3600	0.72	3.46	0.000692	3750	0.75	2.83	0.000566
30	3710	0.742	3.4	0.00068	3770	0.754	2.81	0.000562
35	3580	0.716	3.49	0.000698	3810	0.762	2.8	0.00056
40	3480	0.692	3.47	0.000694	3850	0.77	2.9	0.00058
45	3200	0.64	3.48	0.000696	3890	0.778	2.93	0.000586
50	3210	0.642	3.58	0.000716	3930	0.786	2.96	0.000592
55	3010	0.602	3.57	0.000714	3960	0.792	3.06	0.000612
60	2660	0.532	3.63	0.000726	3950	0.79	3.17	0.000634
65	2370	0.474	3.59	0.000718	3860	0.772	3.33	0.000666
70	2020	0.404	3.54	0.000708	3890	0.738	3.35	0.00067
75	1660	0.332	3.32	0.000664	3340	0.668	3.35	0.00067
80	1140	0.228	2.92	0.000584	2640	0.528	3.12	0.000624
85	490	0.098	1.88	0.000376	1560	0.312	7.7	0.00154

## Narrowing spectral width of green LED by GMR structure to expand color mixing field

S. H. Tu<sup>1</sup>, Y. C. Lee<sup>2</sup>, C. L. Hsu<sup>1</sup>, W. P. Lin<sup>1</sup>, M. L. Wu<sup>1</sup>, T. S. Yang<sup>1</sup>, J. Y. Chang<sup>1</sup>

1. Department of Optical and Photonics, National Central University, Zhongli, Taiwan 32001, ROC

2. Optical Science Center, National Central University, Zhongli, Taiwan, ROC

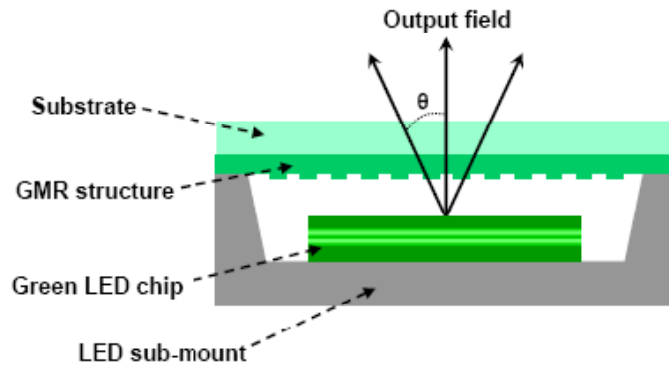


Fig. 2. Illustration of the structural arrangement for reducing the output spectral width of a green LED chip.

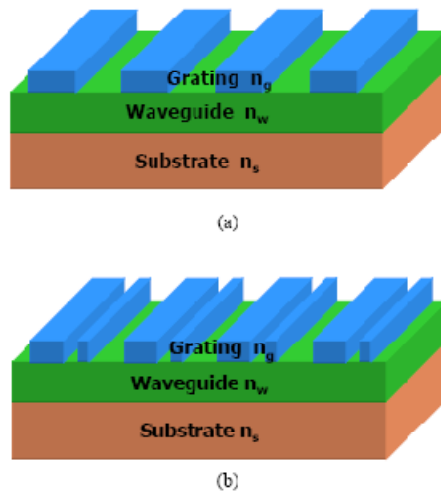
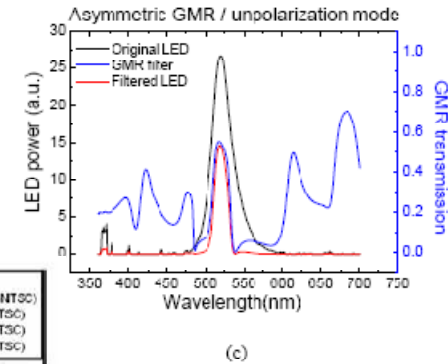
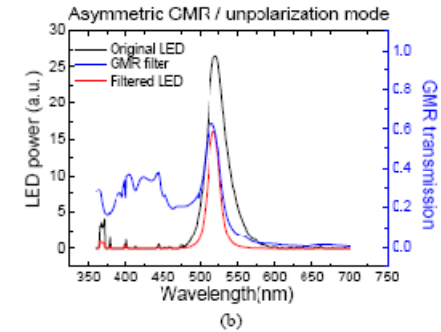
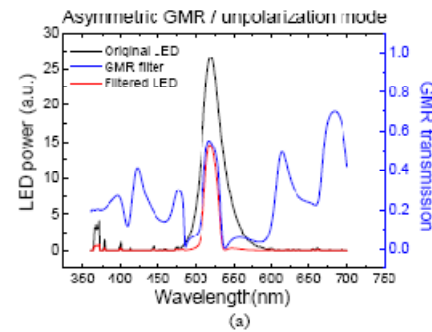
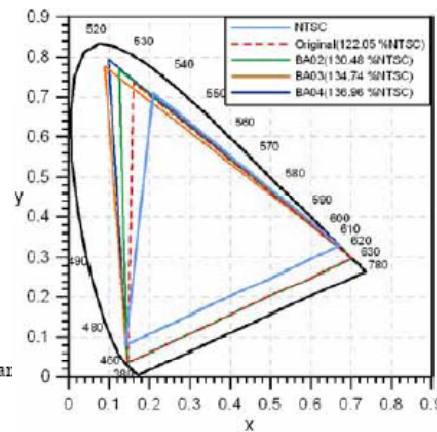


Fig. 1. Illustration of basic GMR filters associated with (a) symmetric and (b) asymmetric grating structures on a planar waveguide constructed transparent substrate.



IR filters associate with an asymmetric grating structure and a LED spectrum with a normally incident unpolarized plane wave. The structure parameters of GMR filters are identical to the structure parameters of GMR filters in Fig. 5.

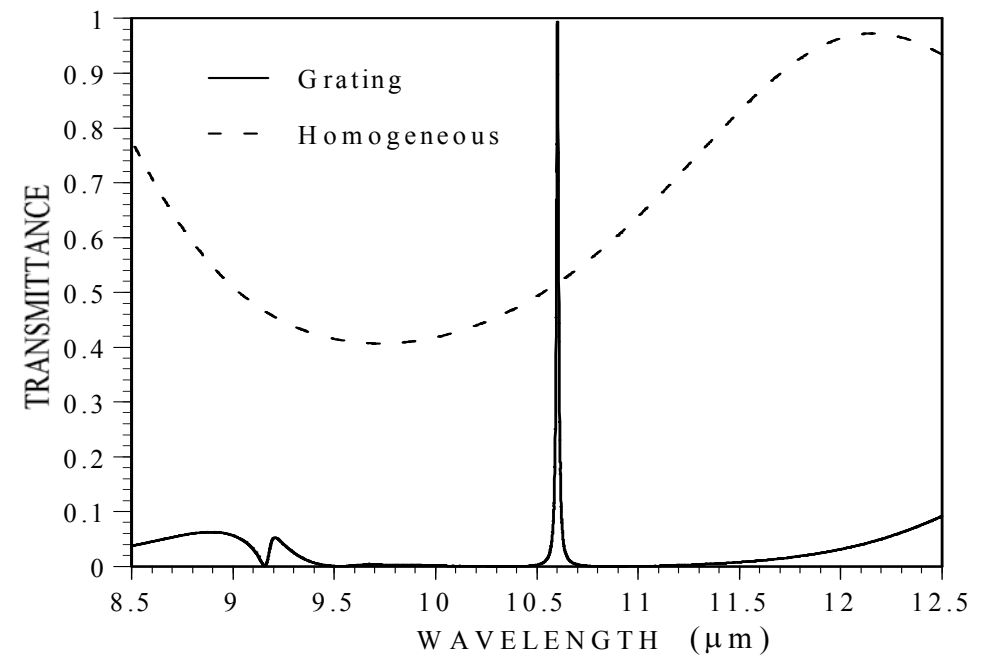
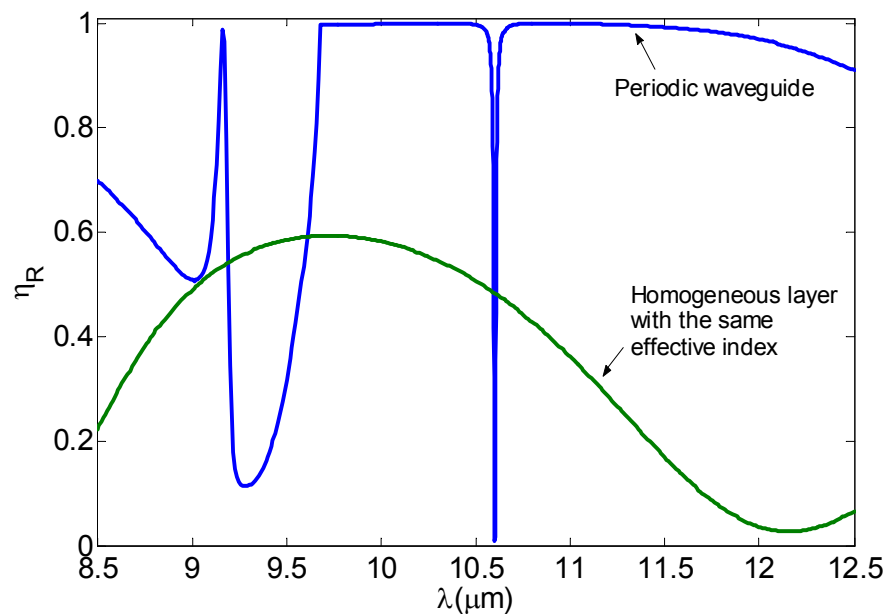
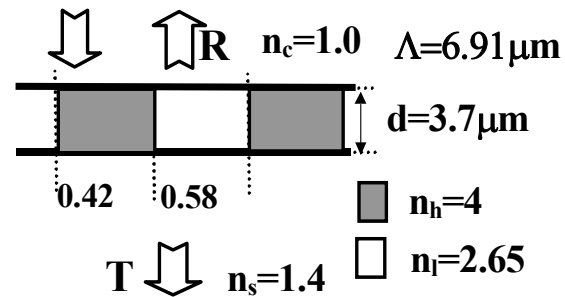




# Narrow-line bandpass filters

R. Magnusson and S. S. Wang, Appl. Optics 34, 8106-8109 (1995).

S. Tibuleac and R. Magnusson, Opt. Lett. 26, 584-586 (2001).



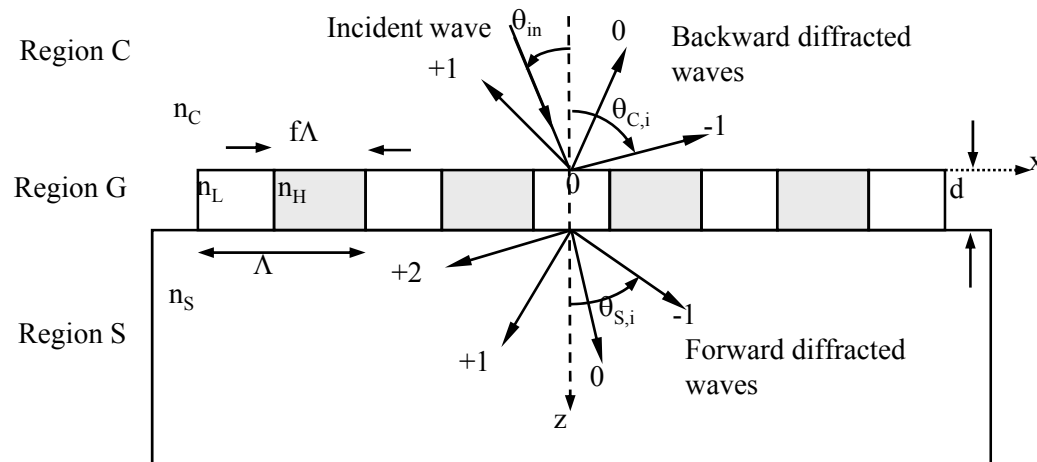


# DIFFRACTIVE OPTICAL ELEMENTS (DOEs) ?

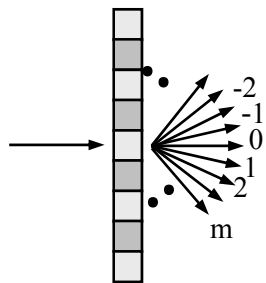
Transmission type

DOE/PhC : Fine spatial patterns arranged to control propagation of light

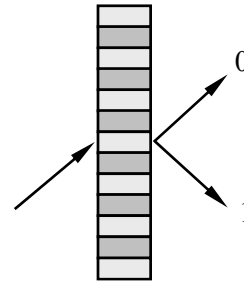
Grating Diffraction



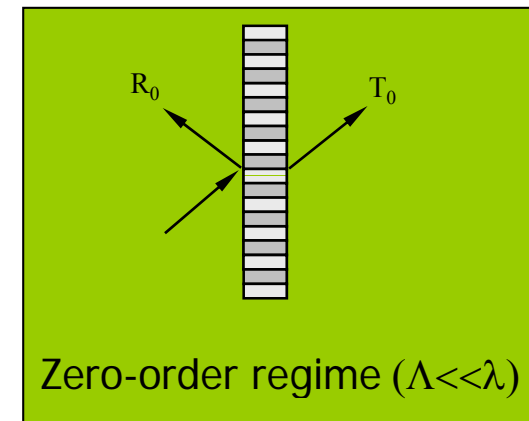
Operating Regimes



$\Lambda(\sin \theta_{in} + \sin \theta_m) = m\lambda$   
Multiwave regime ( $\Lambda \gg \lambda$ )



$2\Lambda \sin \theta_{in} = \lambda$   
Two-wave regime ( $\Lambda \sim \lambda$ )



Zero-order regime ( $\Lambda \ll \lambda$ )

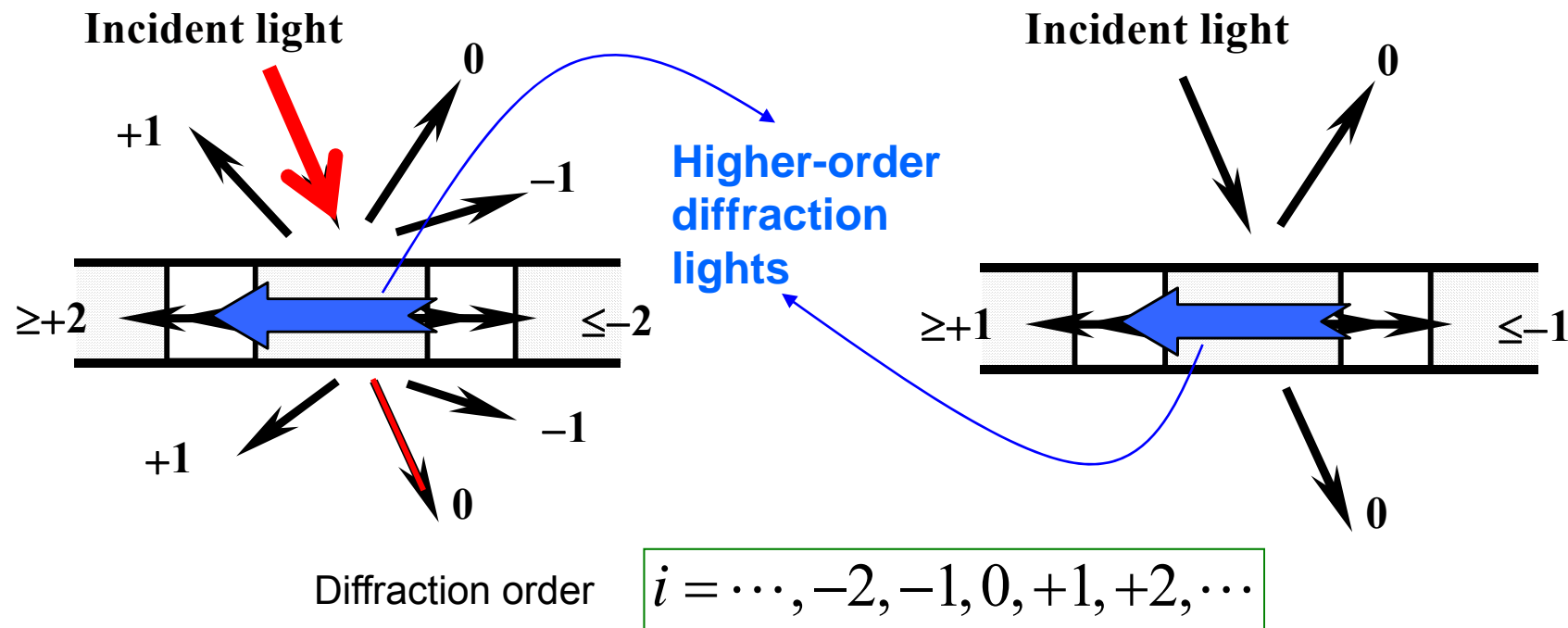
# Basic resonance interactions

Excitation of a leaky guided mode

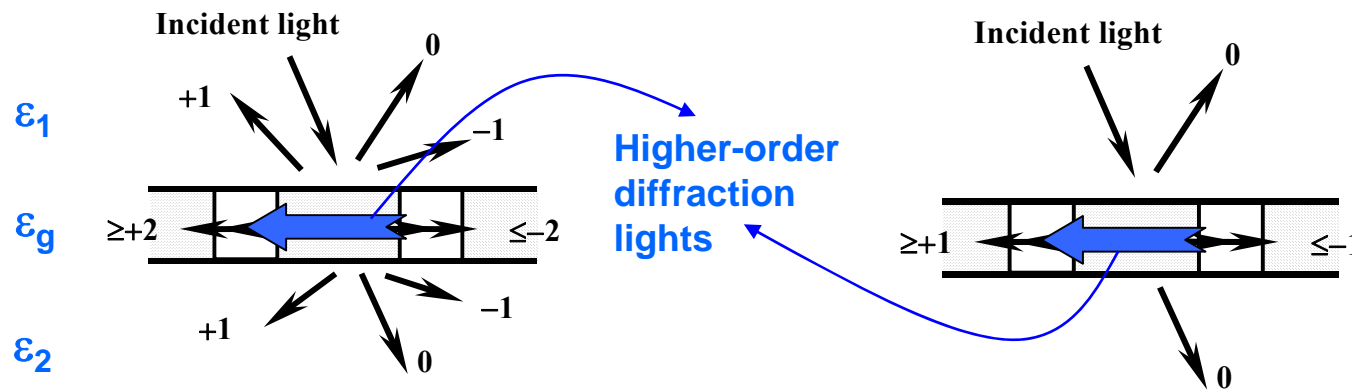
Consider simplest 1D WGG case for clarity

Higher-order diffraction regime

Zero-order diffraction regime



# Guided mode resonance (GMR)



If  $\epsilon_g$  (average dielectric constant)  $> \epsilon_1, \epsilon_2$

the higher-order diffraction lights can be guided on a thin layer of grating.

→ “Guided mode resonance (GMR)” of waveguide gratings

# Basic Concepts of GMR

## Theory and applications of guided-mode resonance filters

S. S. Wang and R. Magnusson APPLIED OPTICS / Vol. 32, No. 14 / 10 May 1993, 2606

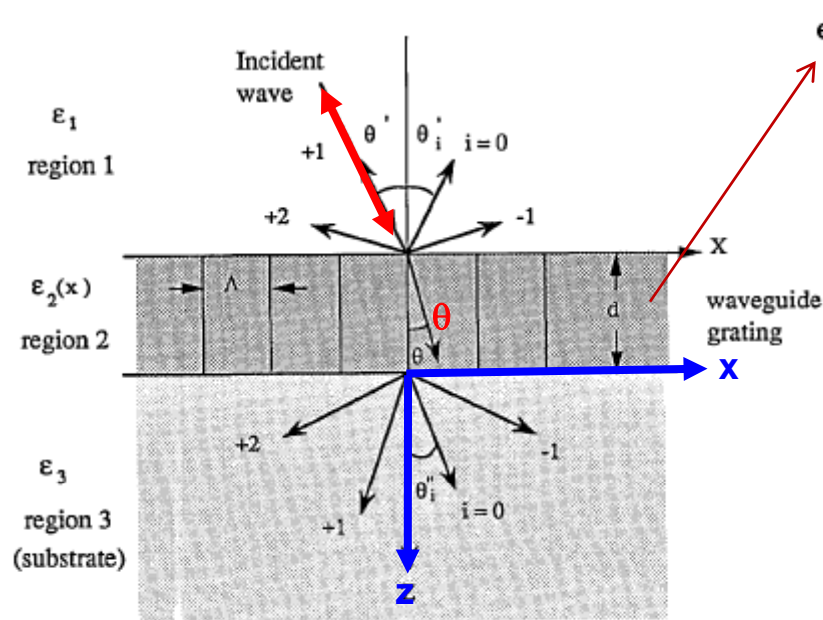


Fig. 1. Basic planar waveguide-grating model used. The angles  $\theta'_i$  represent the angles of the wave vector of the  $i$ th backward-diffracted wave with respect to the  $z$  axis;  $\theta_i$  are the corresponding angles for the forward-diffracted waves. The angle of incidence ( $\theta'$ ) is arbitrary.

$$\epsilon_2(x) = \epsilon_g + \Delta\epsilon \cos Kx$$

$\epsilon_g$  is the average relative permittivity,  
 $\Delta\epsilon$  is the modulation amplitude,  
 $K = 2\pi/\Lambda$ , where  $\Lambda$  is the grating period.

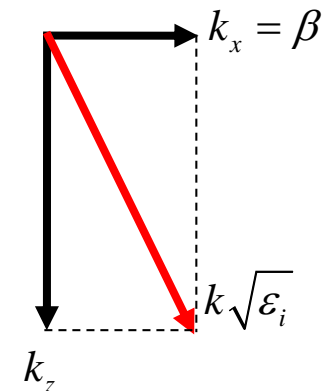
A guided wave can be excited  
 if the effective waveguide index of refraction,  $N$ ,  
 is in the range

$$\max[\sqrt{\epsilon_1}, \sqrt{\epsilon_3}] \leq |N| < \sqrt{\epsilon_g}$$

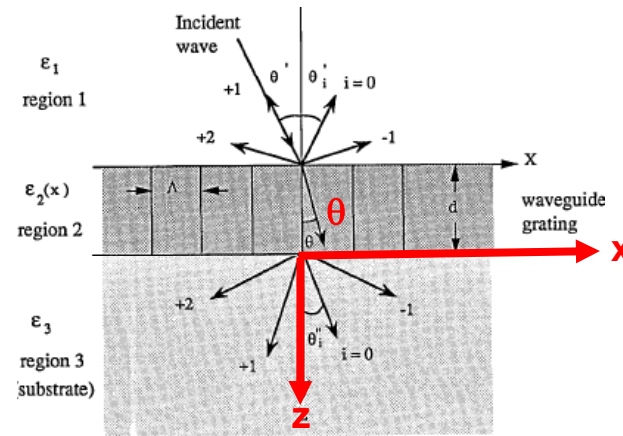
$$N \equiv \frac{\beta}{k} \quad k = \frac{2\pi}{\lambda_0}$$

$$k_x \equiv \beta$$

$$k_z = \sqrt{k^2 \epsilon_g - k_x^2}$$



# Propagation constant of waveguide grating



$$\epsilon_2(x) = \epsilon_g + \Delta\epsilon \cos Kx$$

Coupled-wave equations governing wave propagation in the waveguide grating can be expressed as

$$\frac{d^2 \hat{S}_i(z)}{dz^2} + [k^2 \epsilon_g - k_2^2 (\sqrt{\epsilon_g} \sin \theta - i\lambda/\Lambda)^2 \hat{S}_i(z) + \frac{1}{2} k^2 \Delta\epsilon [\hat{S}_{i+1}(z) + \hat{S}_{i-1}(z)]] = 0, \quad (1)$$

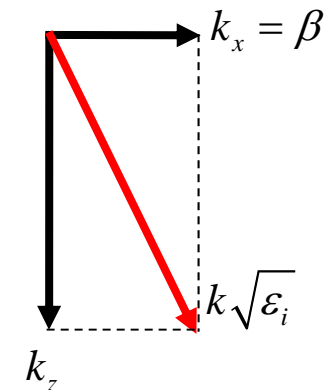
where  $\hat{S}_i$  is the amplitude of the inhomogeneous plane wave of the  $i$ th space harmonic

As  $\Delta\epsilon \rightarrow 0$ , the wave equation associated with an unmodulated dielectric waveguide is given by

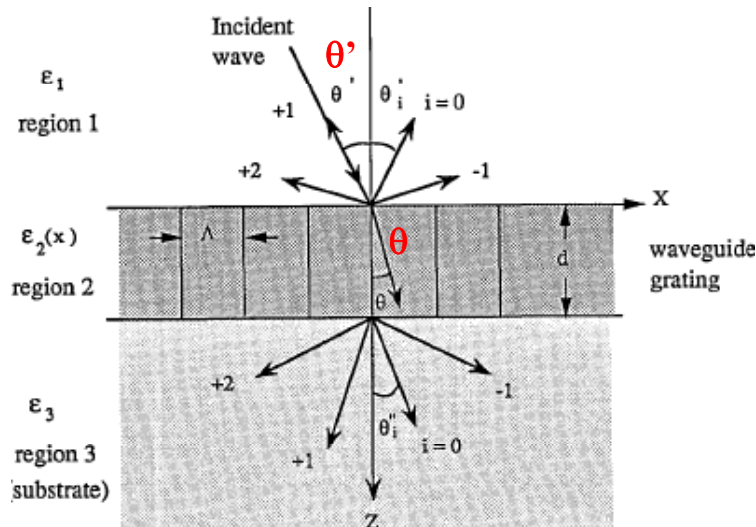
$$\frac{d^2 E(z)}{dz^2} + (k^2 \epsilon_g - \beta^2) E(z) = 0, \quad (2) \quad k_z = \sqrt{k^2 \epsilon_g - k_x^2} \quad (k_x = \beta)$$

Letting  $\Delta\epsilon \rightarrow 0$  in Eq. (1) and by direct comparison with Eq. (2), we obtain the effective propagation constant of the waveguide grating:

$$\beta \rightarrow \beta_i = k(\sqrt{\epsilon_g} \sin \theta - i\lambda/\Lambda) \quad \text{Propagation constant}$$



# Diffraction equation of waveguide grating



$$\max\{\sqrt{\epsilon_1}, \sqrt{\epsilon_3}\} \leq |N| < \sqrt{\epsilon_g}$$

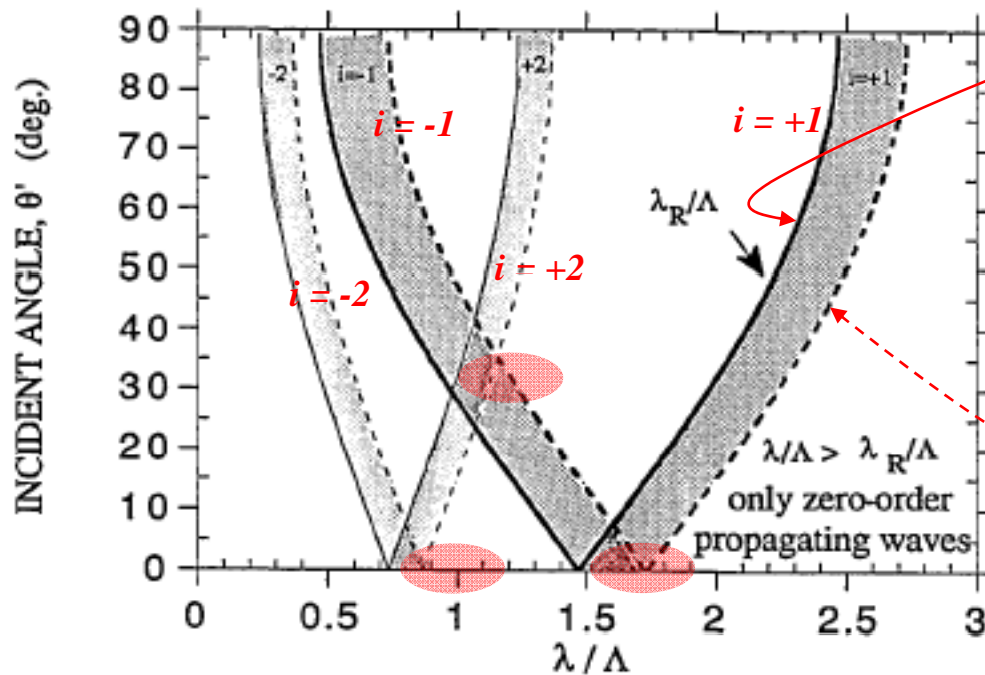
$$\beta \rightarrow \beta_i = k(\sqrt{\epsilon_g} \sin \theta - i\lambda/\Lambda)$$

where we use  $\sqrt{\epsilon_1} \sin \theta' = \sqrt{\epsilon_g} \sin \theta$ , with  $\theta'$  being the external angle of incidence,



$$\max\{\sqrt{\epsilon_1}, \sqrt{\epsilon_3}\} \leq |\sqrt{\epsilon_1} \sin \theta' - i\lambda/\Lambda| < \sqrt{\epsilon_g}$$

**Diffraction equation**



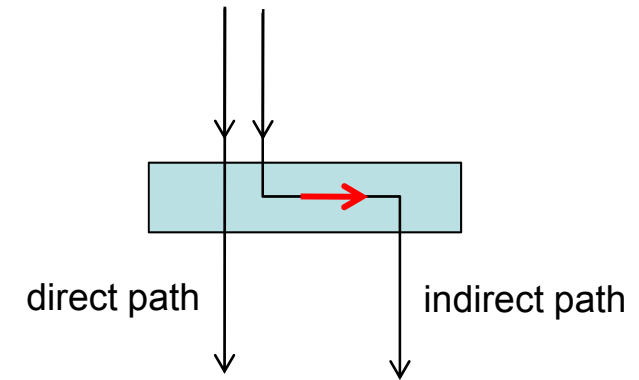
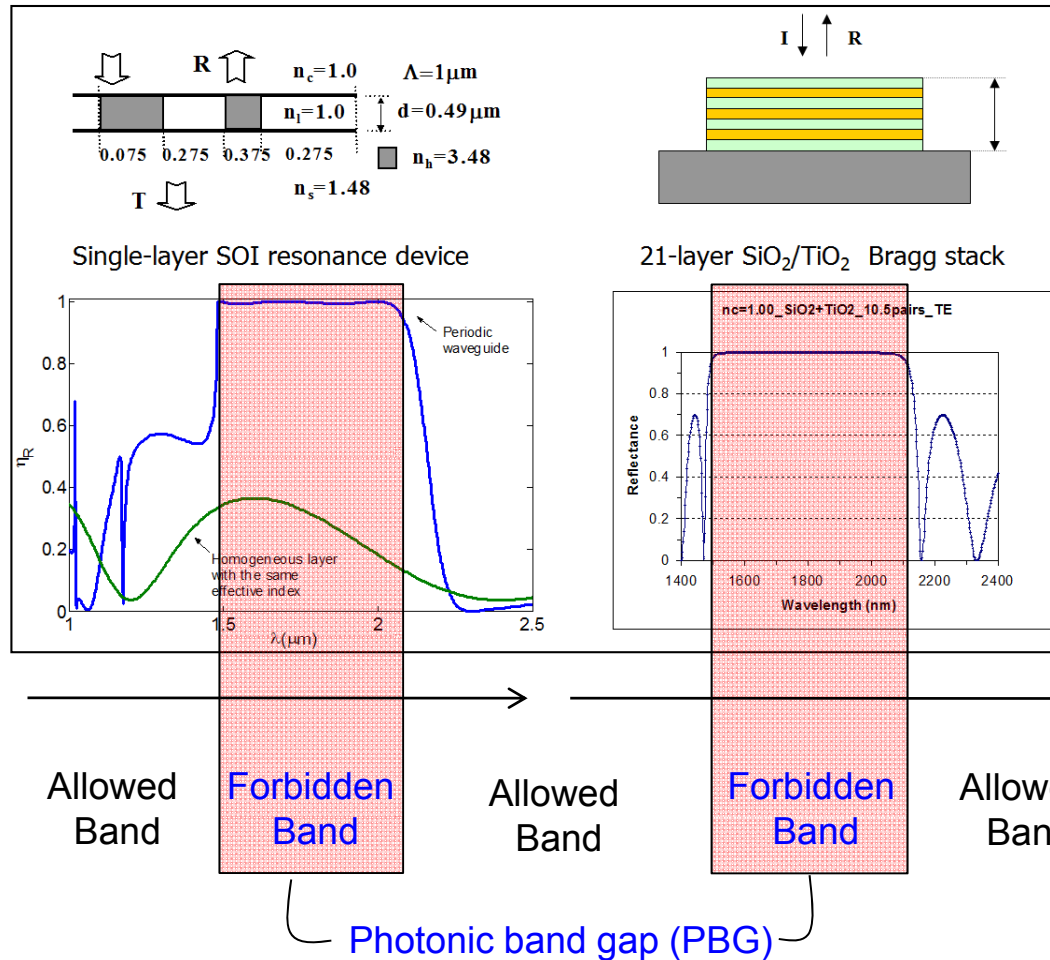
$$\max\{\sqrt{\epsilon_1}, \sqrt{\epsilon_3}\} = \left| \sqrt{\epsilon_1} \sin \theta' - i \frac{\lambda}{\Lambda} \right|$$

$$\left| \sqrt{\epsilon_1} \sin \theta' - i \frac{\lambda}{\Lambda} \right| < \sqrt{\epsilon_g}$$

Fig. 3. Resonance regimes of waveguide gratings. The parameters are  $\epsilon_1 = 1$ ,  $\epsilon_g = 3$ , and  $\epsilon_3 = 2.161$ .

## GMR filters

How to intuitively understand the GMR effect, for example, in mirrors?



**Constructive/destructive Interference**

**Photonic band structure**

No transmission of light within the bandgap due to destructive interference in transmitted light.



# Photonic band structure is analogous to energy-band structure of electrons

## Photons and Electrons

*Nanophotonics, Paras N. Prasad, 2004, John Wiley & Sons, Inc., Hoboken, New Jersey., ISBN 0-471-64988-0*

Both photons and electrons are elementary particles that simultaneously exhibit particle and wave-type behavior.

Photons and electrons may appear to be quite different as described by classical physics, which defines photons as electromagnetic waves transporting energy and electrons as the fundamental charged particle (lowest mass) of matter.

A quantum description, on the other hand, reveals that photons and electrons can be treated analogously and exhibit many similar characteristics.

**Table 2.1.** Similarities in Characteristics of Photons and Electrons

Photons	Electrons
<b>Wavelength</b>	
$\lambda = \frac{h}{p} = \frac{c}{\nu}$	$\lambda = \frac{h}{p} = \frac{h}{mv}$
<b>Eigenvalue (Wave) Equation</b>	
$\left\{ \nabla \times \frac{1}{\epsilon(r)} \nabla \times \right\} \mathbf{B}(r) = \left( \frac{\omega}{c} \right)^2 \mathbf{B}(r)$	$\hat{H}\psi(r) = -\frac{\hbar^2}{2m}(\nabla \cdot \nabla + V(r))\psi(r) = E\psi$
<b>Free-Space Propagation</b>	
Plane wave $\mathbf{E} = \left( \frac{1}{\epsilon} \right) \mathbf{E}^0 (e^{i\mathbf{k} \cdot \mathbf{r} - \omega t} + e^{-i\mathbf{k} \cdot \mathbf{r} + \omega t})$ $\mathbf{k}$ = wavevector, a real quantity	Plane wave: $\Psi = c(e^{i\mathbf{k} \cdot \mathbf{r} - \omega t} + e^{-i\mathbf{k} \cdot \mathbf{r} + \omega t})$ $\mathbf{k}$ = wavevector, a real quantity
<b>Interaction Potential in a Medium</b>	
Dielectric constant (refractive index)	Coulomb interactions
<b>Propagation Through a Classically Forbidden Zone</b>	
Photon tunneling (evanescent wave) with wavevector, $\mathbf{k}$ , imaginary and hence amplitude decaying exponentially in the forbidden zone	Electron-tunneling with the amplitude (probability) decaying exponentially in the forbidden zone
<b>Localization</b>	
Strong scattering derived from large variations in dielectric constant (e.g., in photonic crystals)	Strong scattering derived from a large variation in Coulomb interactions (e.g., in electronic semiconductor crystals)
<b>Cooperative Effects</b>	
Nonlinear optical interactions	Many-body correlation Superconducting Cooper pairs Biexciton formation

## Consider free-space propagation of photons and electrons.

In a “free-space” propagation, there is no interaction potential or it is constant in space. For photons, it simply implies that no spatial variation of refractive index  $n$  occurs.

The wavevector dependence of energy is different for photons (linear dependence) and electrons (quadratic dependence).

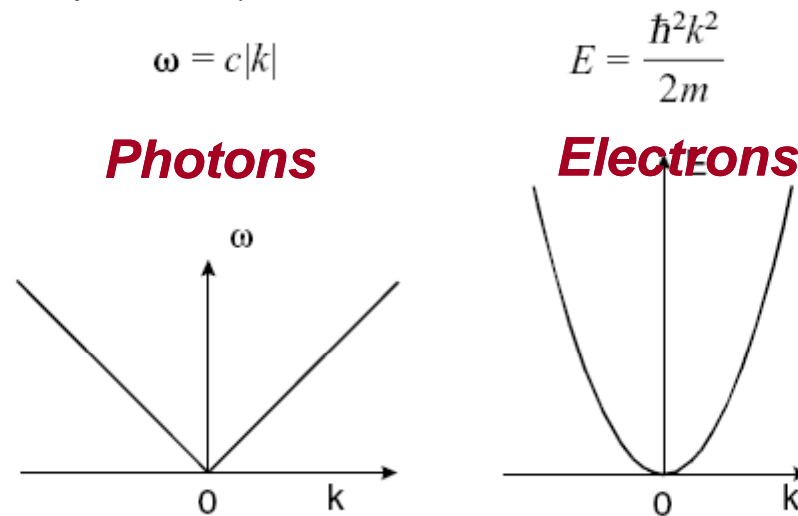
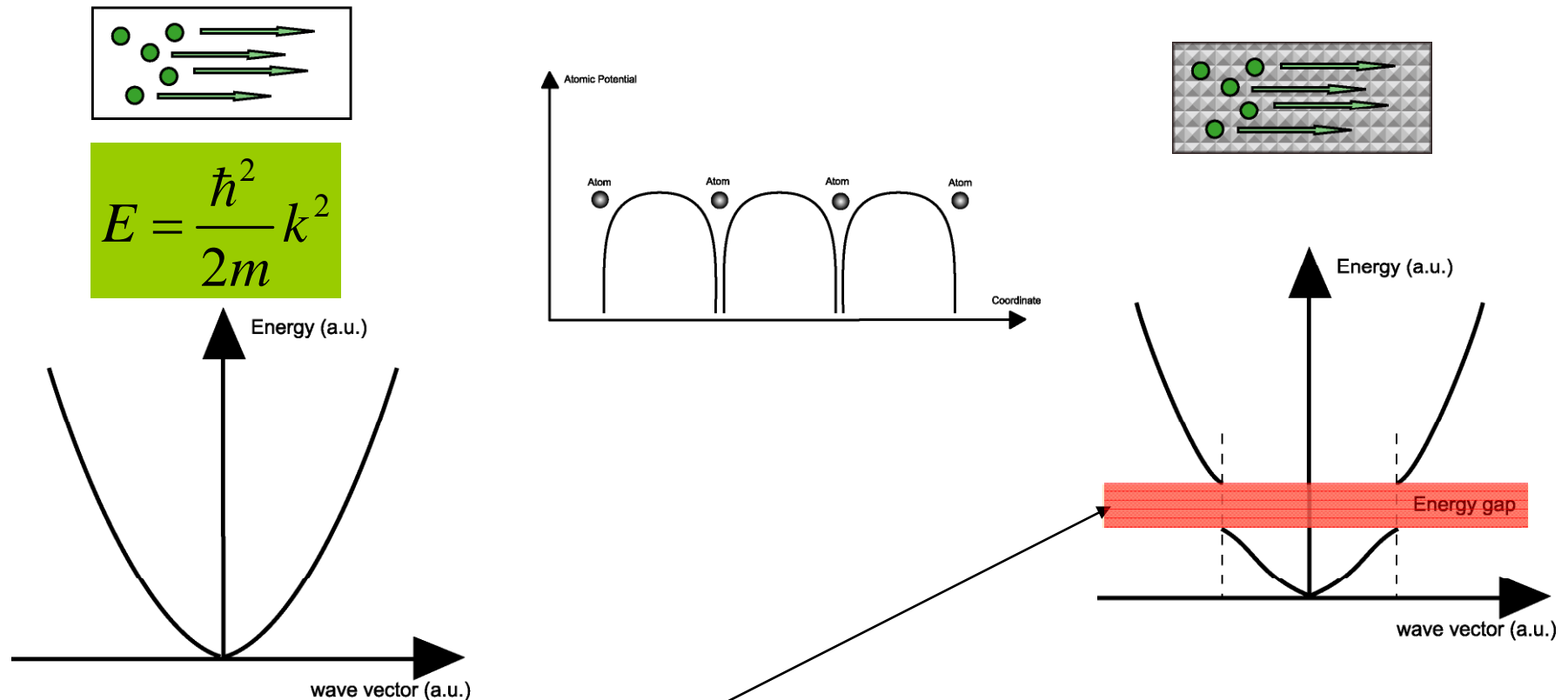


Figure 2.1. Dispersion relation showing the dependence of energy on the wavevector for a free-space propagation. (a) Dispersion for photons. (b) Dispersion for electrons.

For free-space propagation, all values of frequency for photons and energy for electrons are permitted. This set of allowed continuous values of frequency (or energy) form together a band. The **band structure** refers to the characteristics of dependence of frequency  $\omega$  (or energy) on wavevector  $k$ , called **dispersion relation**.

**Energy band structure = Dispersion relation ( $\omega$ - $k$  relation)**

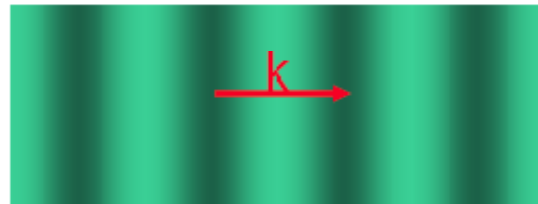
Photonic bandgap (PBG) is analogous to electron energy bandgap



Gap in energy spectra of electrons arises in periodic structure

## A simple example of the band-structure: vacuum (1d)

Vacuum:  $\epsilon=1$ ,  $\mu=1$ , plane-wave solution to the Maxwell's equation:



$$\mathbf{H} e^{i(\mathbf{k} \cdot \mathbf{r} - \omega t)}$$

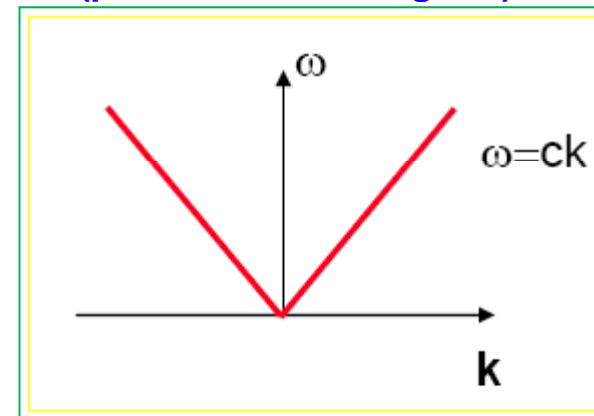
with a transversality constraints:  $\mathbf{k} \cdot \mathbf{H} = 0$

A band structure, or dispersion relation defines the relation between the frequency  $\omega$ , and the wavevector  $\mathbf{k}$ .

$$\omega = c|\mathbf{k}|$$

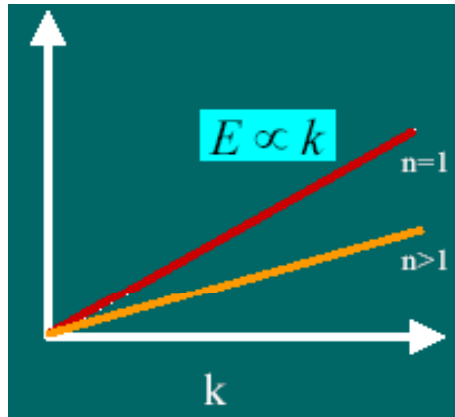
For a one-dimensional system, the band structure can be simply depicted as:

Dispersion curve  
(photonic band diagram)



## PBG formation by periodic structures

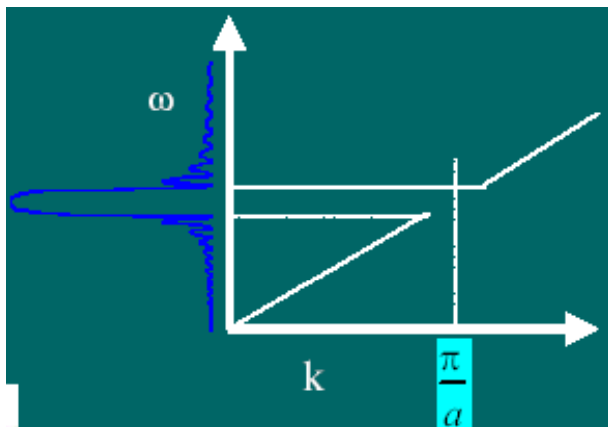
1. Dispersion curve for free space



2. In a periodic system, when half the wavelength corresponds to the periodicity

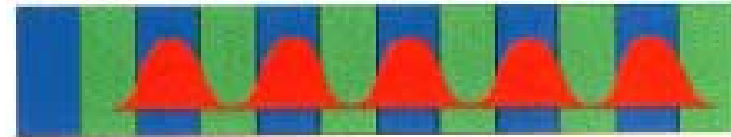
$$\lambda/2 = a \quad k = \pi/a$$

the Bragg effect prohibits photon propagation.

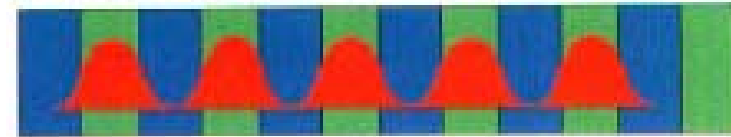


3. At the band edges, standing waves form, with the energy being either in the high or the low index regions

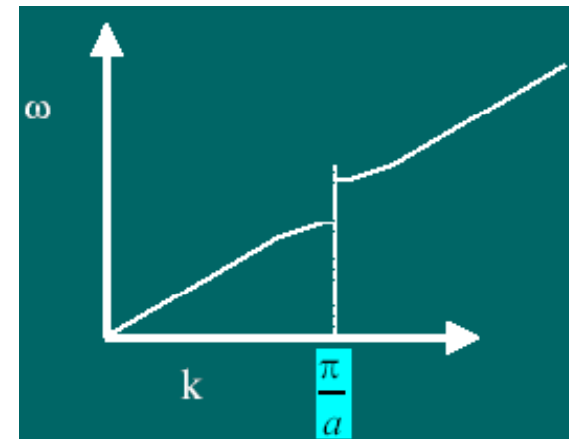
Local power in E-field, top of band 1



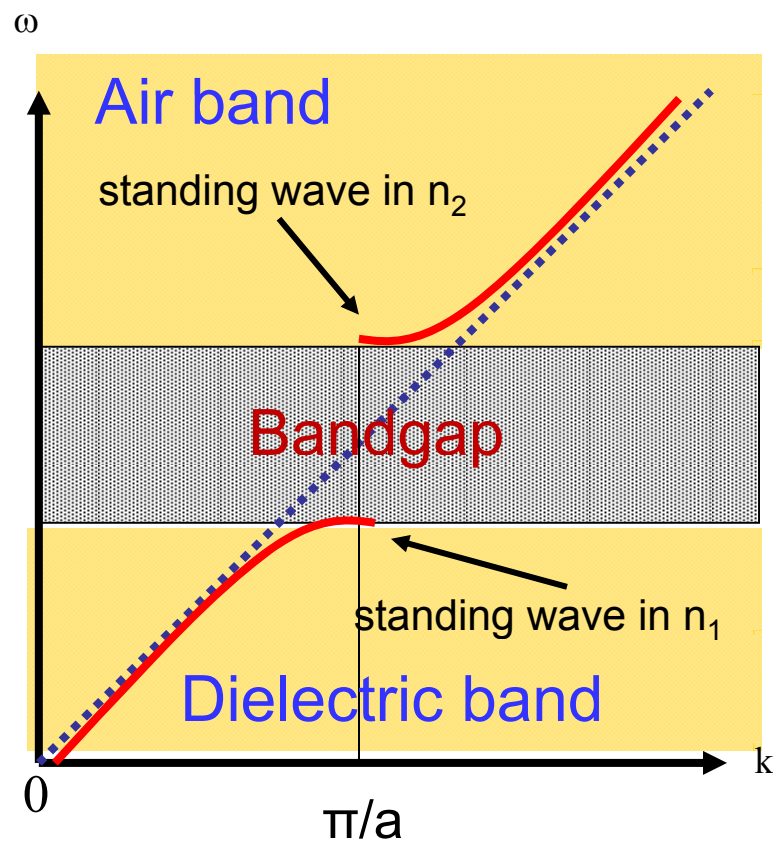
Local power in E-field, bottom of band 2



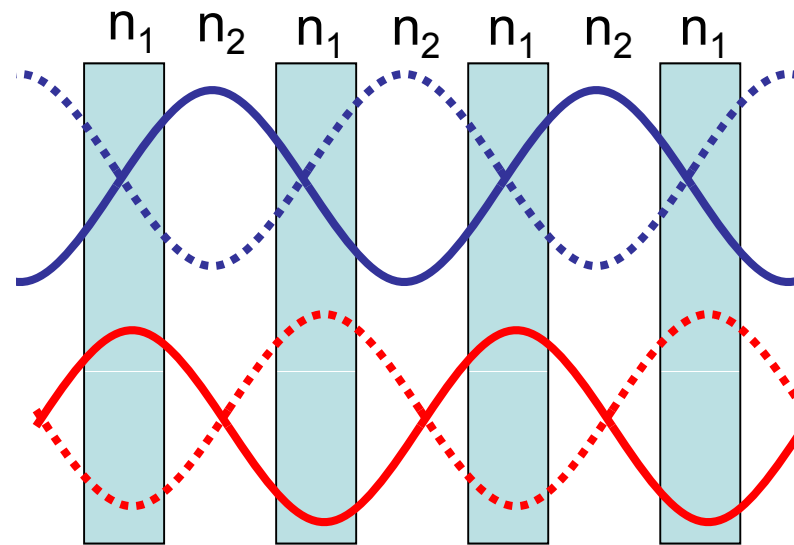
4. Standing waves transport no energy with zero group velocity



## Standing waves at band edges



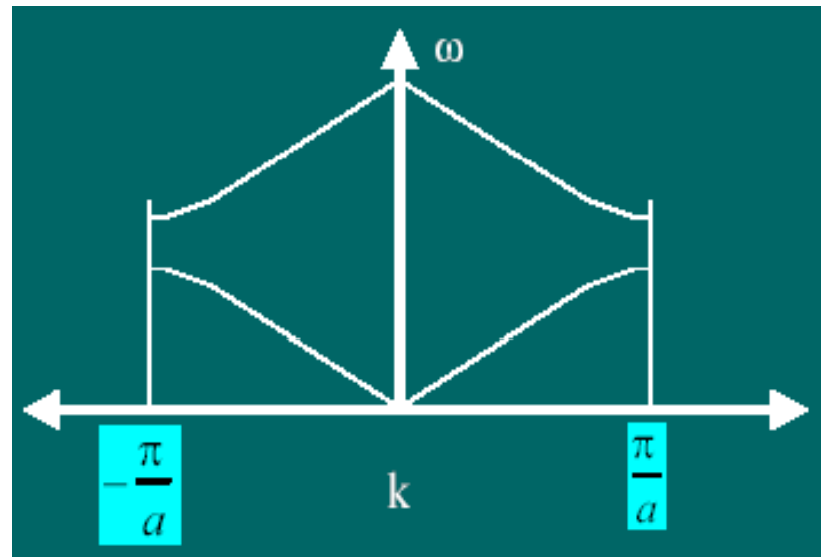
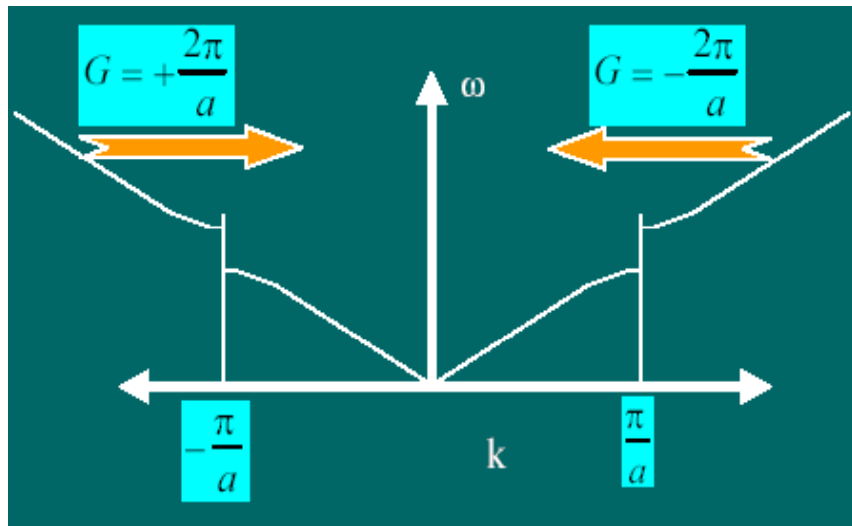
Standing waves with zero group velocity



$n_1$ : high index material  
 $n_2$ : low index material

# Reduced Brillouin zone

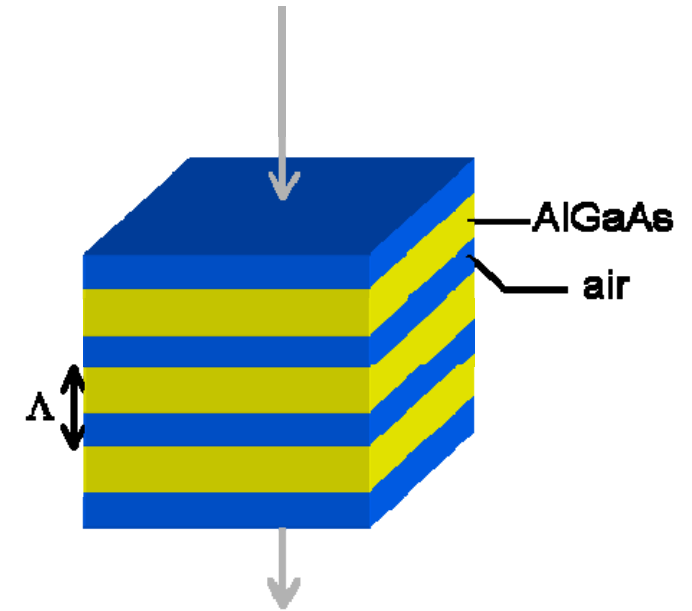
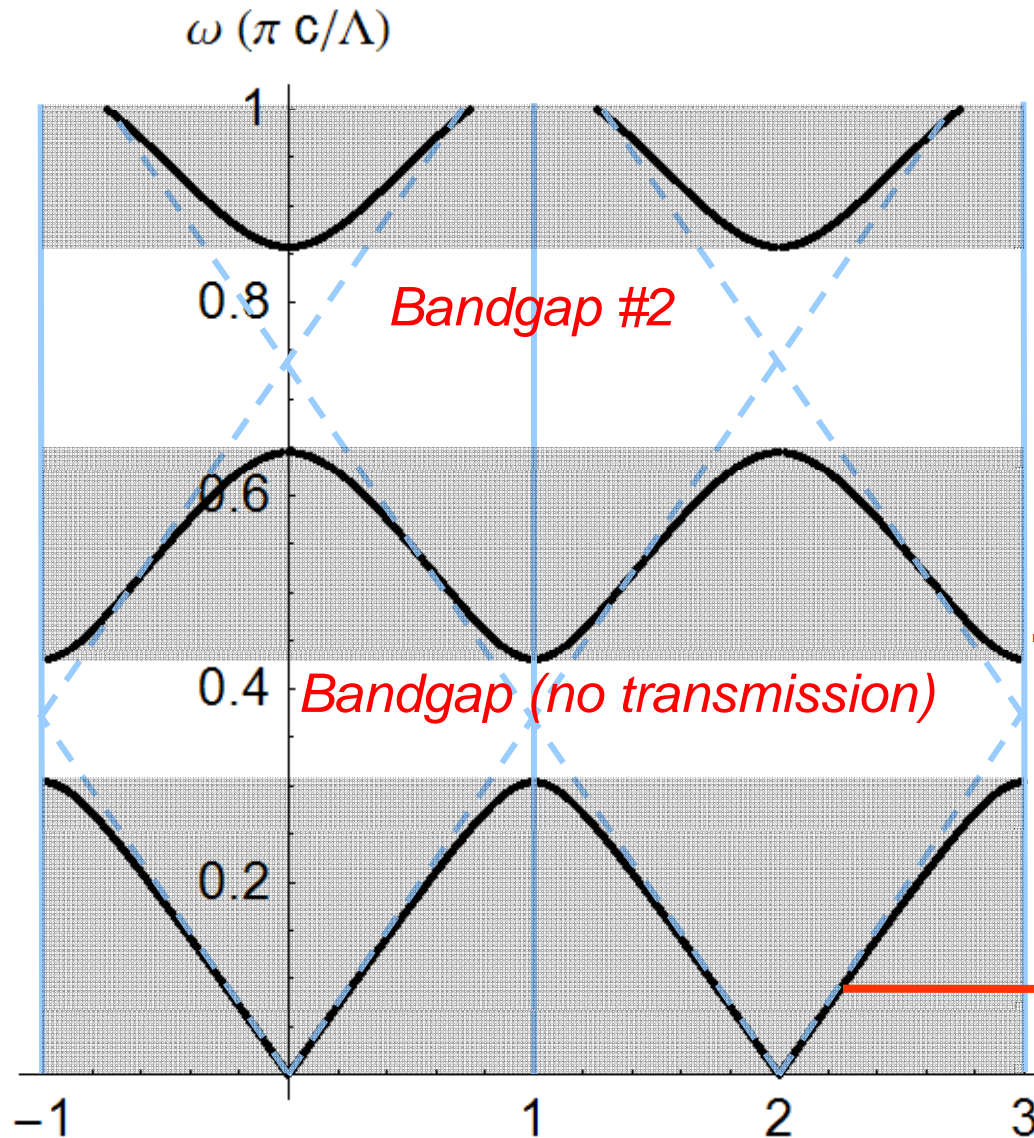
Plot the dispersion curves for both the positive and the negative sides, and then shift the curve segments with  $|k| > \pi/a$  upward or downward one reciprocal lattice vectors.



This reduced range of wave vectors is called the “**Brillouin zone**”



# Photonic Band Gaps (PBG)



Standing wave

$v_{\text{group}} = 0$

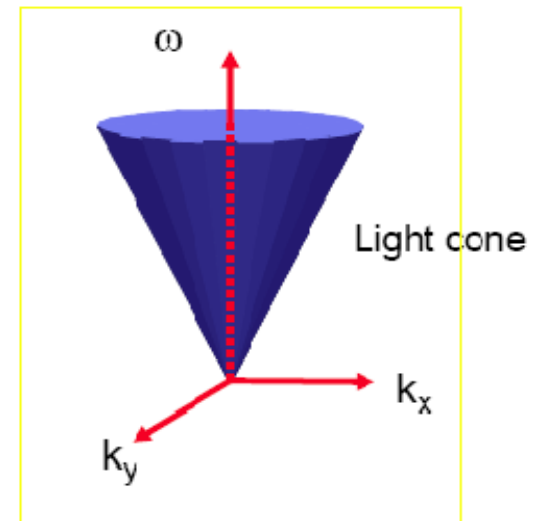
Long wavelength  
limit: effective index

## Visualization of the vacuum band structure (2d)

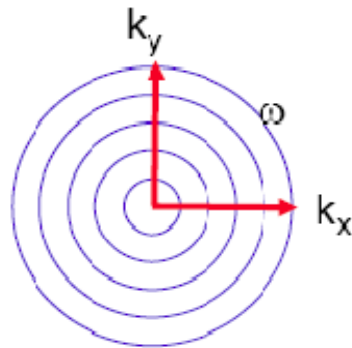
For a two-dimensional system:

$$\omega = c\sqrt{k_x^2 + k_y^2}$$

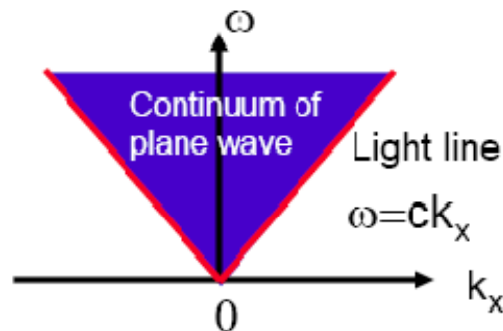
This function depicts a cone: light cone.



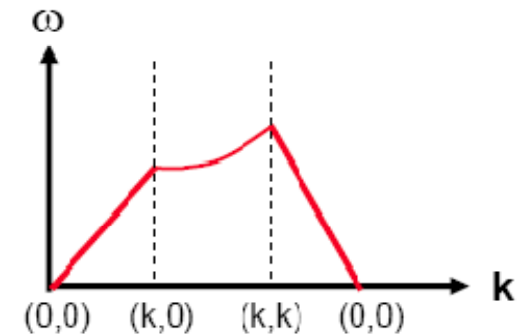
A few ways to visualize this band structure :



Constant frequency contour



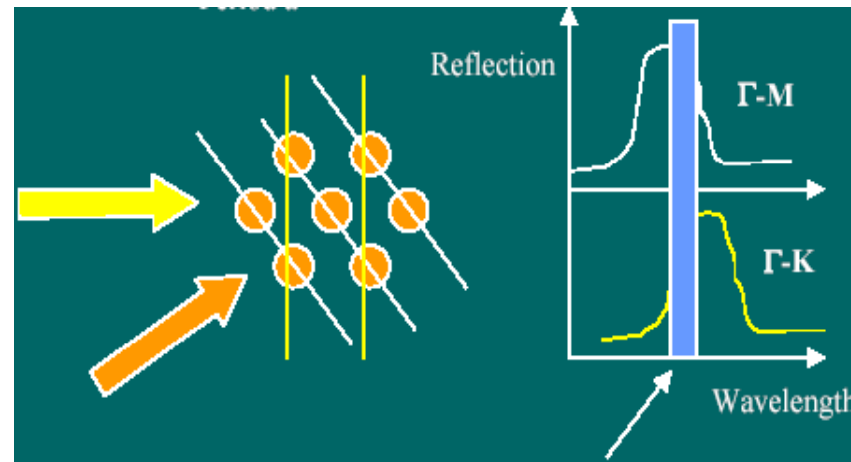
Projected band diagram



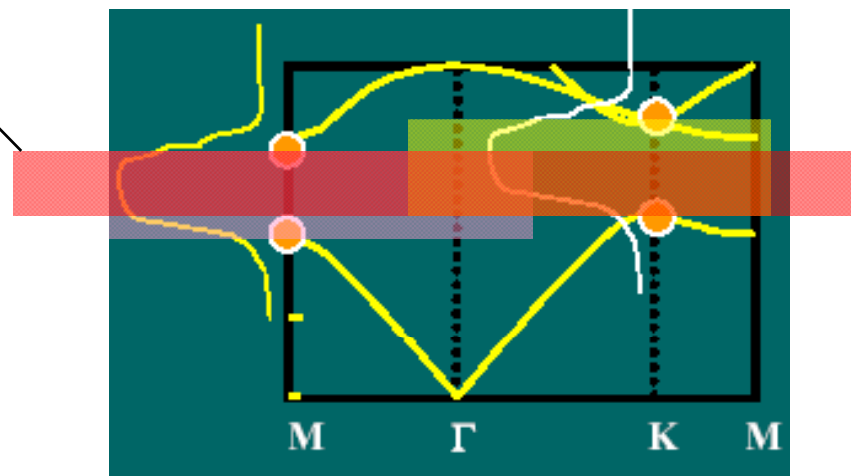
Band diagram along  
several "special"  
directions

# 2-D Photonic Crystals

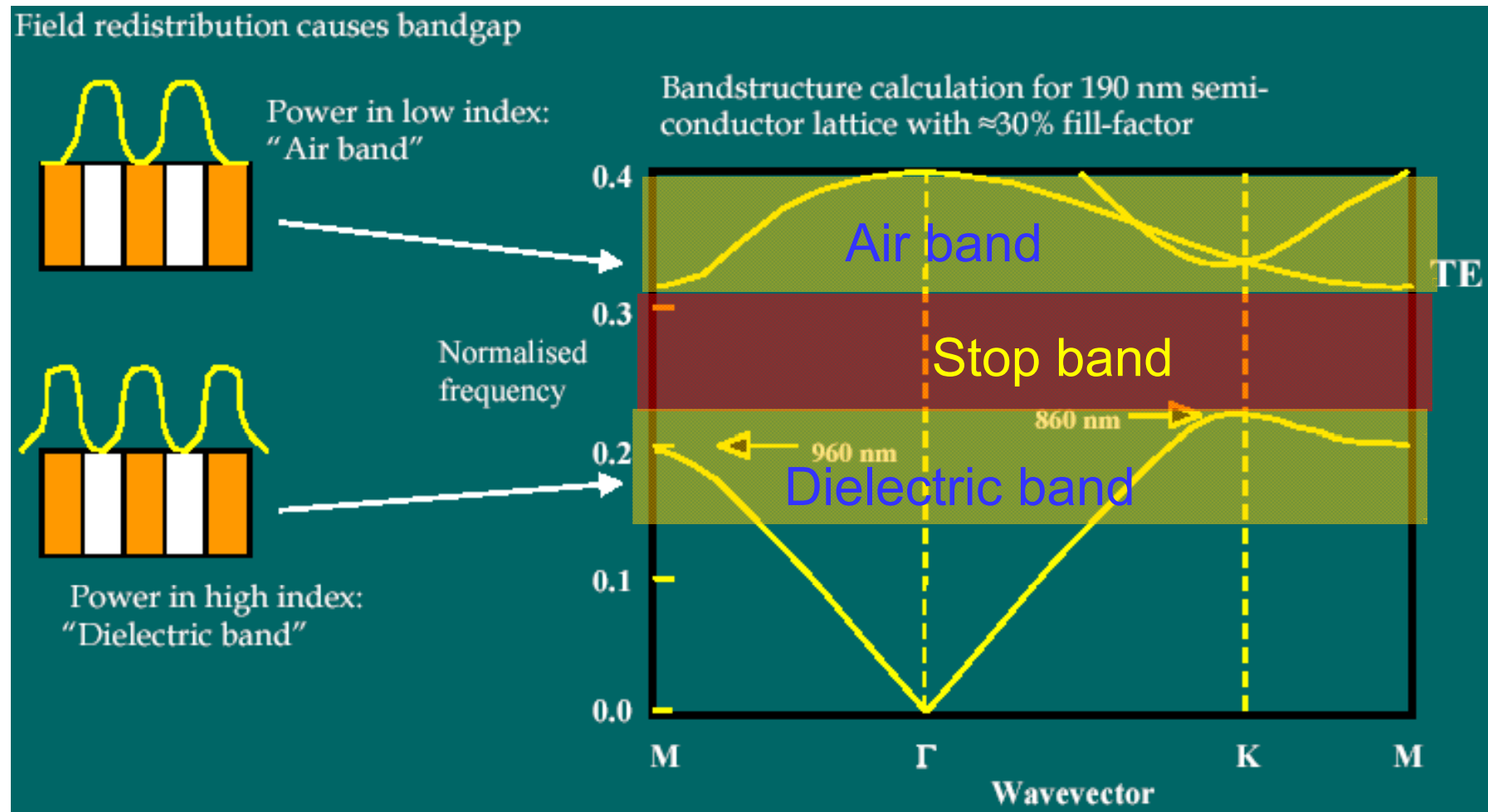
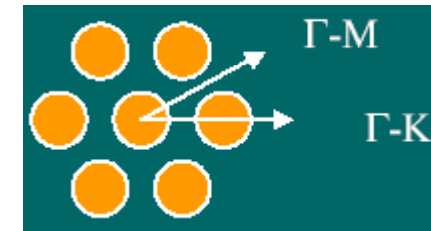
1. In 2-D PBG, different layer spacing,  $a$ , can be met along different direction. Strong interaction occurs when  $\lambda/2 = a$ .



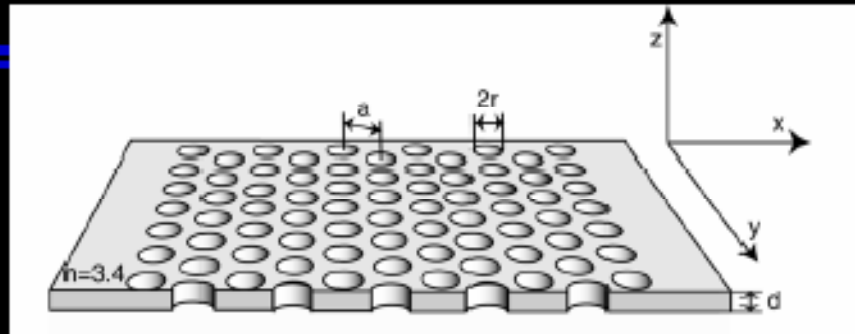
2. PBG (Photonic band gap) = stop bands overlap in all directions



# Band Diagram

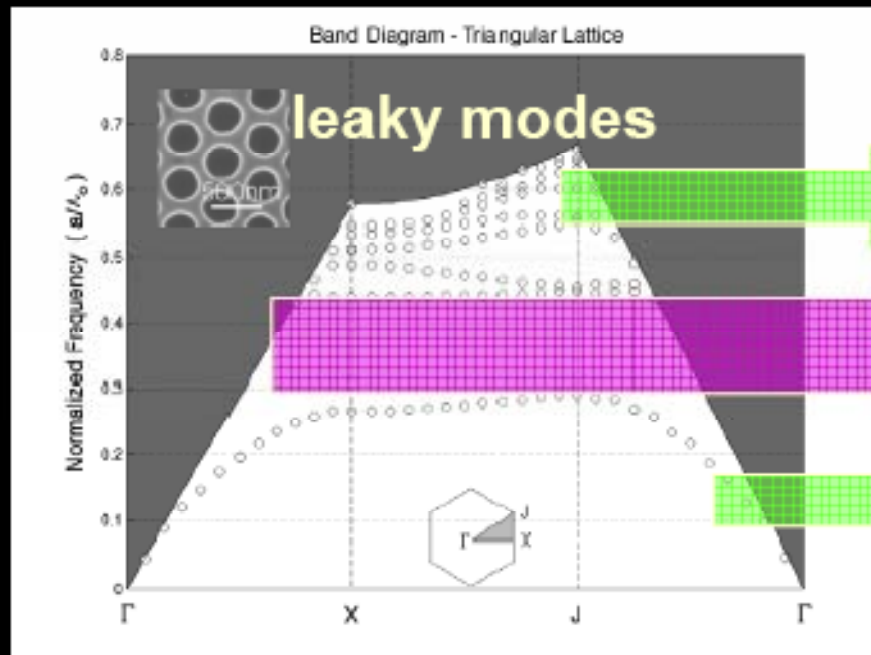


## Band structure of a two-dimensional crystal



Dispersion diagram is determined by:

- $r$  (hole radius)
- $a$  (periodicity of lattice)
- $d$  (slab thickness)
- $n$  (refractive index:  $3.4 < n < 3.5$ )
- lattice type



guided modes  
(air band)

band gap

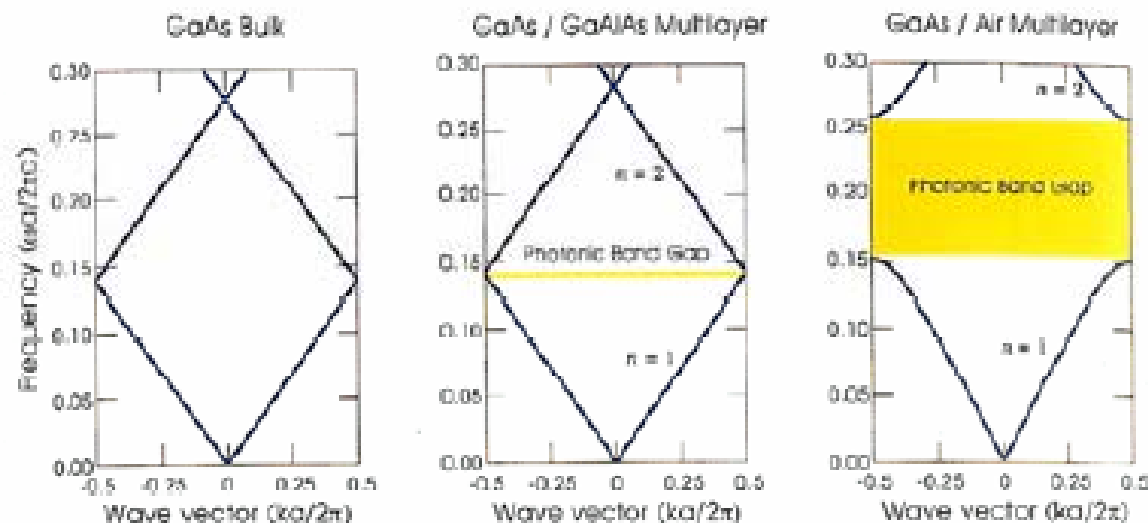
guided modes  
(dielectric band)

### Contrast dependent band gap

Magnitude of the bandgap depends on index contrast

No contrast, no reflections, no gap

Weak contrast, reflected beam only enhanced if many interfaces contribute with *exactly the correct phase*: highly frequency selective: small gap



**Figure 2** The photonic band structures for on-axis propagation, shown for three different multilayer films, all of which have layers of width  $0.5a$ . Left: each layer has the same dielectric constant  $\epsilon = 13$ . Center: layers alternate between  $\epsilon = 13$  and  $\epsilon = 12$ . Right: layers alternate between  $\epsilon = 13$  and  $\epsilon = 1$ .

From: *Photonic Crystals – Molding the flow of light*, Joannopoulos, Meade, and Winn

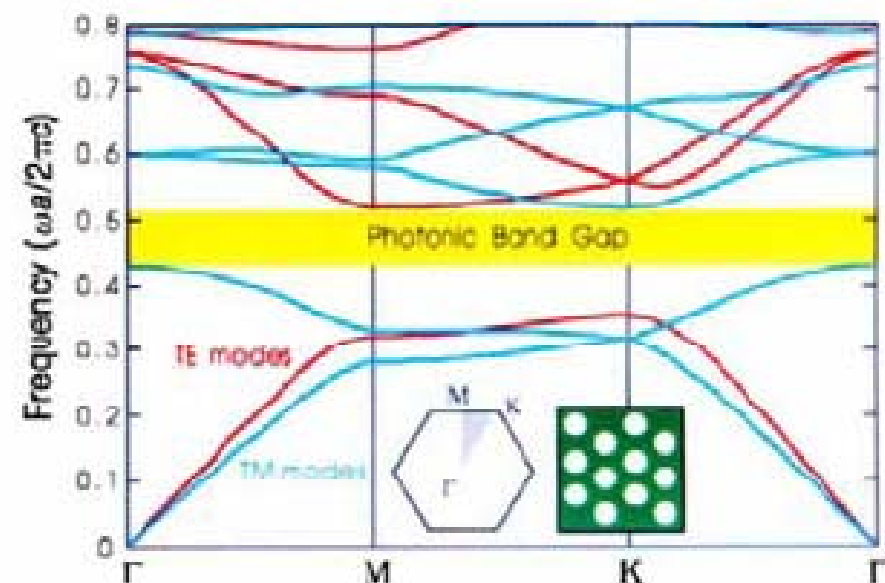
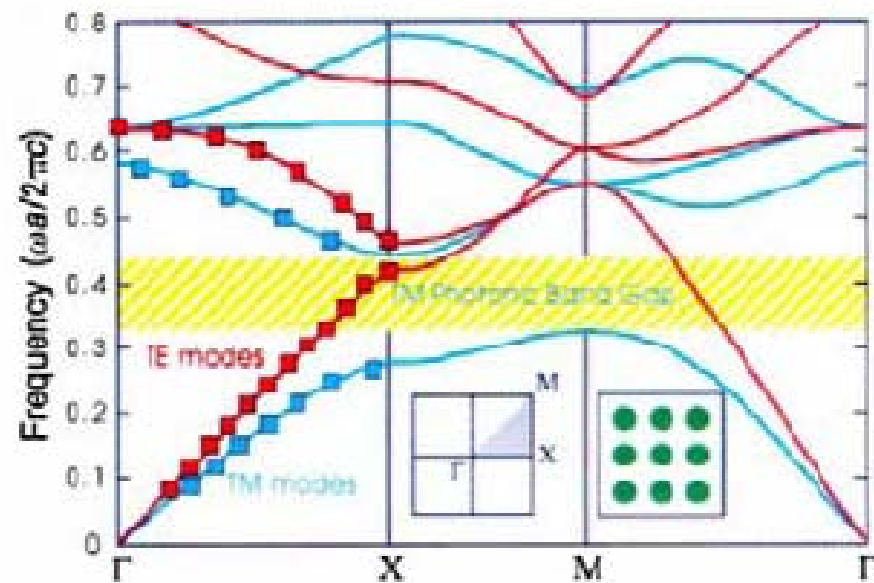
# Angular dependence vs. photonic crystal lattice

2D structures: dispersion relation angle dependent

Similar to phonons in atomic lattices or electrons in periodic potentials

(but without exclusion principle!)

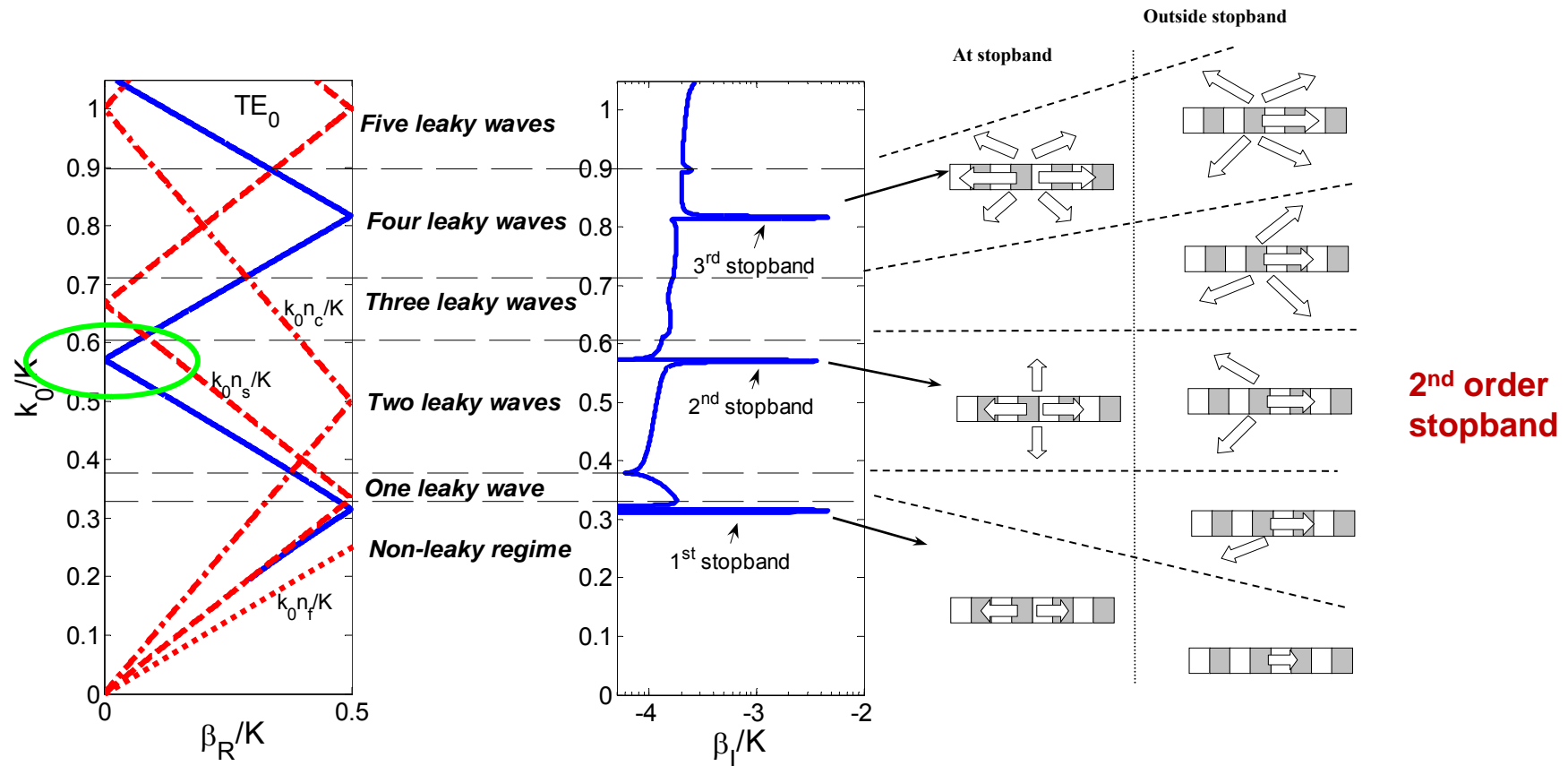
Joannopoulos, JD, Villeneuve, PR & Fan, S. Photonic crystals: putting a new twist on light. *Nature* 386, 143-149 (1997)



**Figure 1** Top, photonic band structure for a square lattice of dielectric ( $\epsilon = 8.9$ ) rods in air with radius  $r = 0.2a$ , where  $a$  is the lattice constant. TM modes are shown in blue and TE modes in red. The solid lines are from theory and the squares represent experimental measurements along  $\Gamma$  to X from Robertson *et al.* Bottom, photonic band structure for a triangular lattice of air cylinders ( $r = 0.48a$ ) in dielectric ( $\epsilon = 13$ ). Note the presence of a complete photonic bandgap for both TE and TM polarizations in this case as shown by a solid yellow bar. In both panels high-dielectric material is indicated in green in the insets.



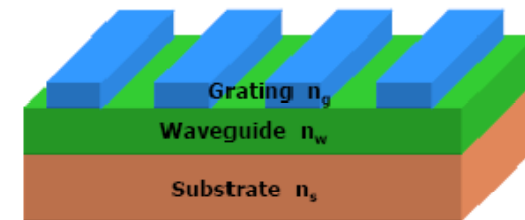
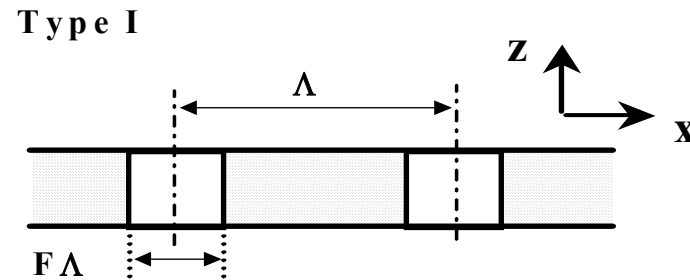
# Photonic bandgaps (stop bands) in GMR gratings



Complex propagation constant of leaky mode  $\beta = \beta_R + j \beta_I$

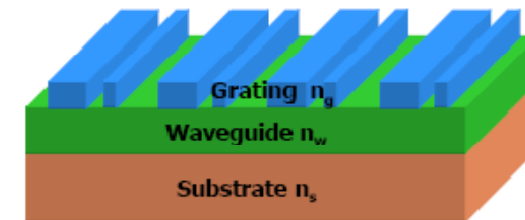
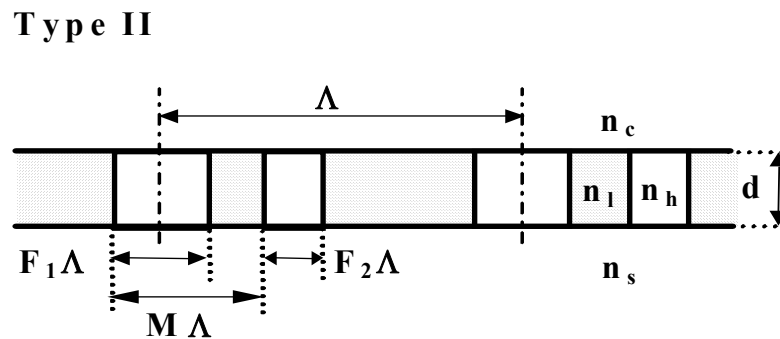
# Symmetry in grating profile of GMR elements

(a) Grating with symmetric profile



(a)

(b) Grating with asymmetric profile



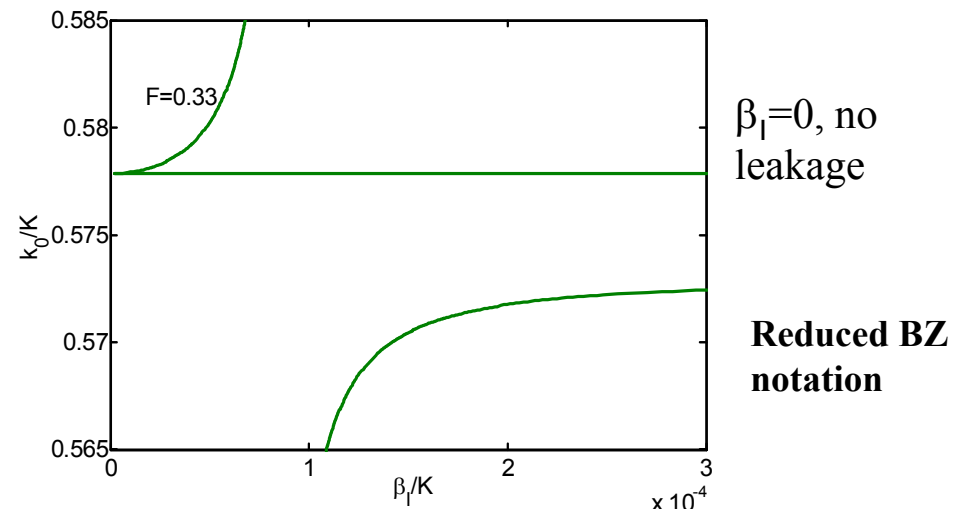
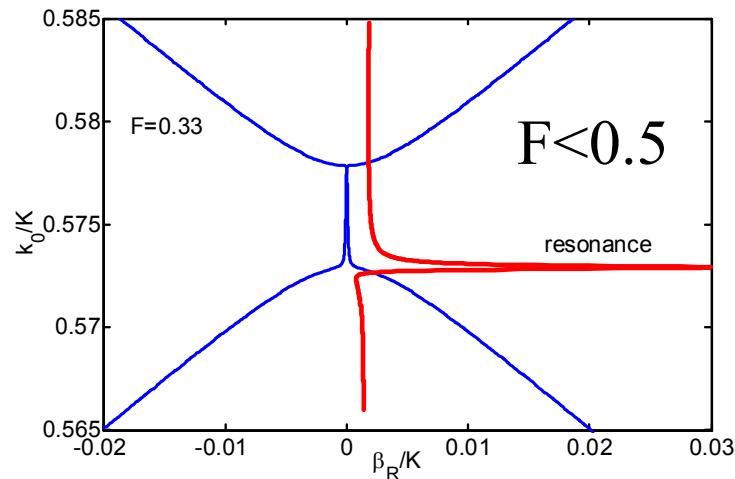
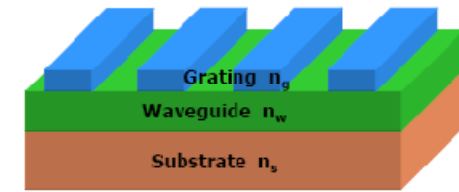
(b)

Fig. 1. Illustration of basic GMR filters associated with (a) symmetric and (b) asymmetric grating structures on a planar waveguide constructed on a transparent substrate.

Details: Y. Ding and R. Magnusson, "Use of nondegenerate resonant leaky modes to fashion diverse optical spectra," Optics Express, May 3, 2004

# Symmetric profile band diagram

Complex propagation constant of leaky mode  $\beta = \beta_R + j \beta_I$



Vincent/Neviere 1979: Asymmetry “defeats selection rule”

P. Vincent and M. Nevier, “Corrugated dielectric waveguides: A numerical study of the second-order stop bands,” Appl. Phys. **20**, 345-351 (1979).

Perturbation model:  $0, \pi$  phase differences of radiated fields (symmetric profile)

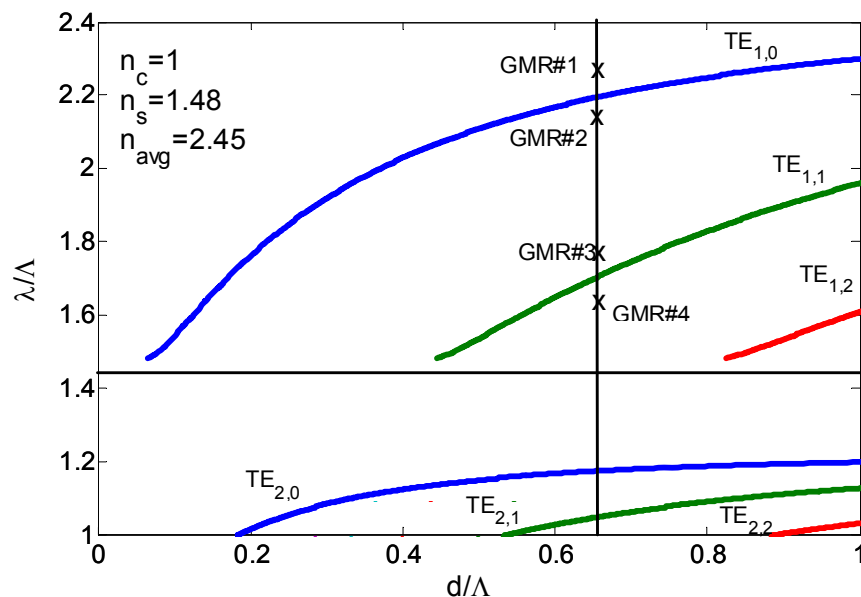
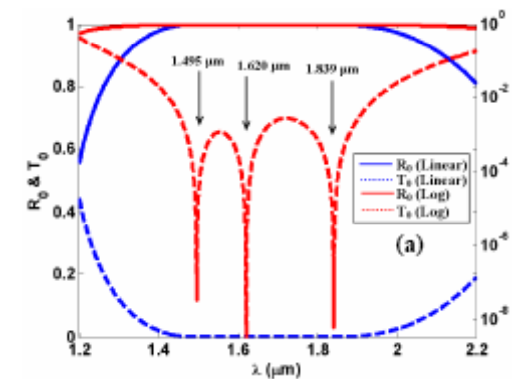
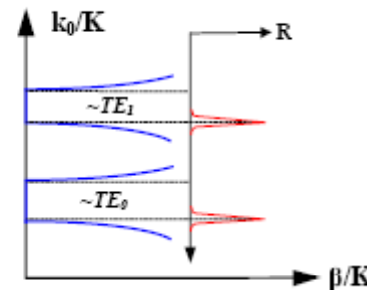
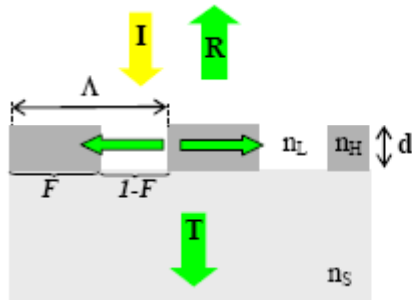
R. F. Kazarinov and C. H. Henry, “Second-order distributed feedback lasers with mode selection provided by first-order radiation loss,” IEEE J. Quant. Elect. **QE-21**, 144-150 (1985).

Numerical calculations of resonance at edges (symmetric profile)

D. L. Brundrett, E. N. Glytsis, T. K. Gaylord, and J. M. Bendickson, “Effects of modulation strength in guided-mode resonant subwavelength gratings at normal incidence,” J. Opt. Soc. Am. A. **17**, 1221-1230 (2000).

# Design of multi-resonance elements

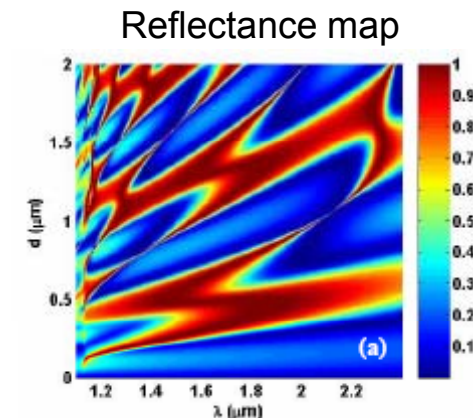
- Resonance locations are estimated with the eigenfunction of homogeneous waveguide (modulation  $\sim 0$ )
- Numerical RCWA computations



Notation:

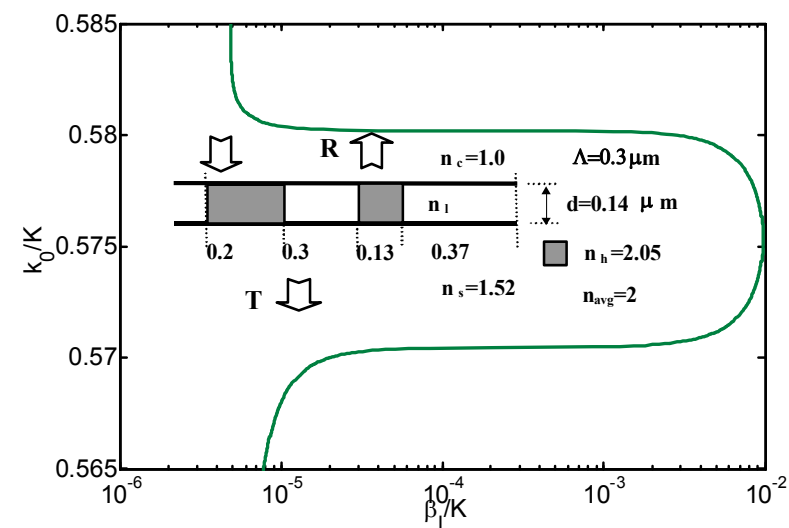
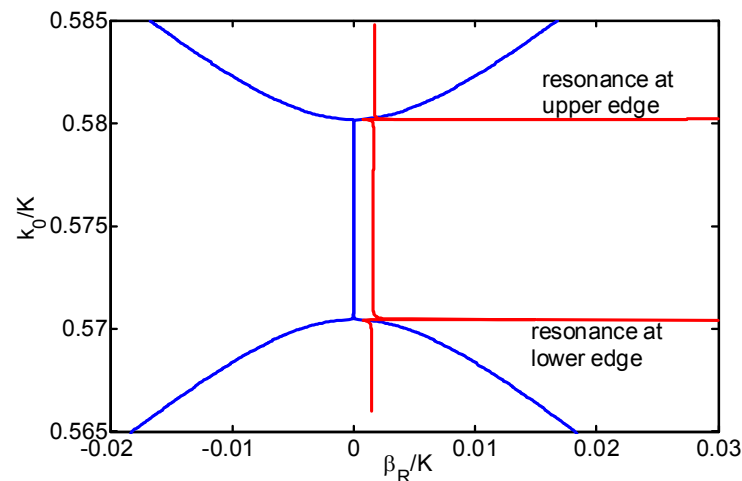
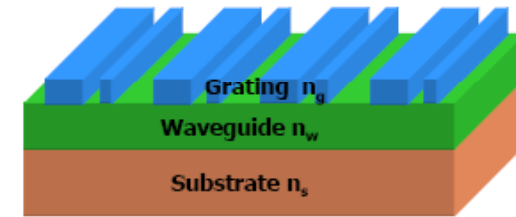
$TE_{m,v}$

$m$  represents the evanescent diffraction order exciting the  $v$ -th mode



# Band diagram of asymmetric profile

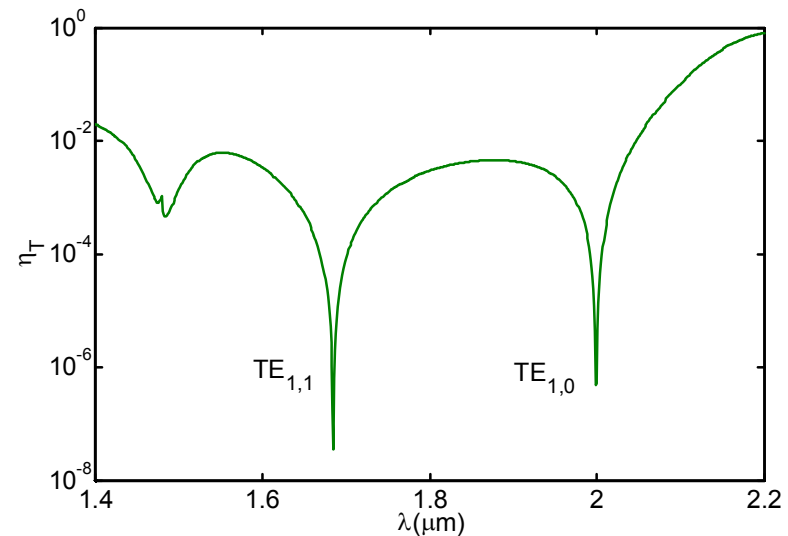
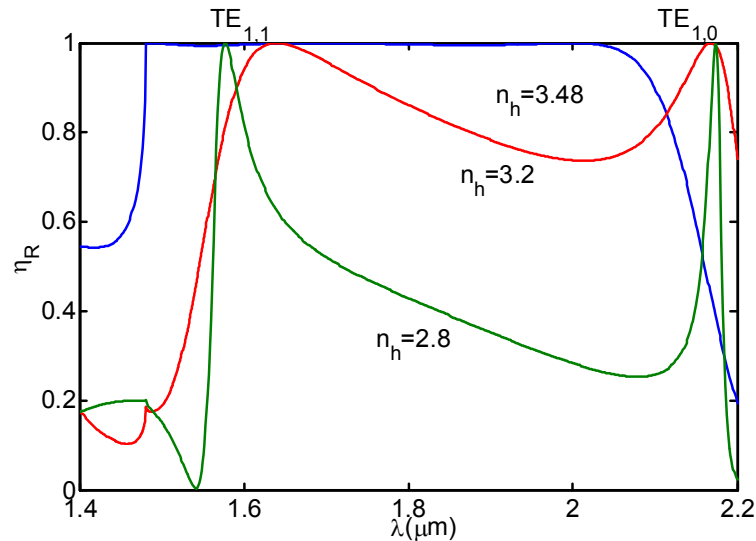
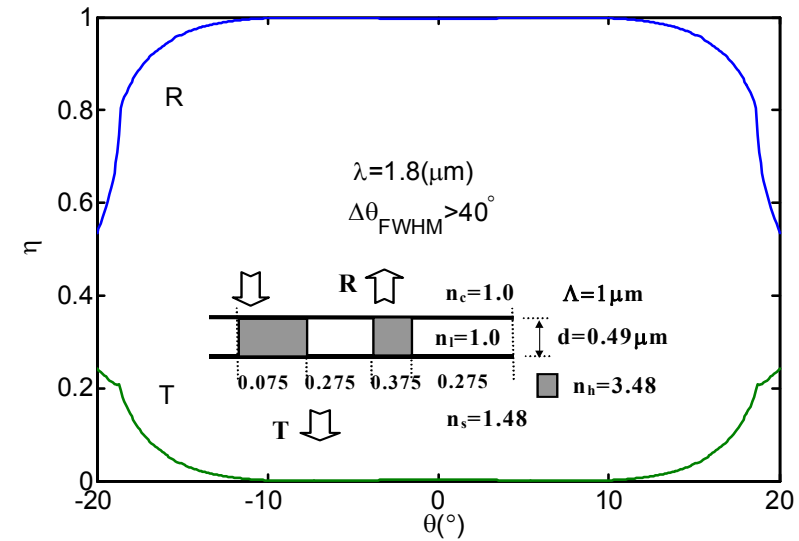
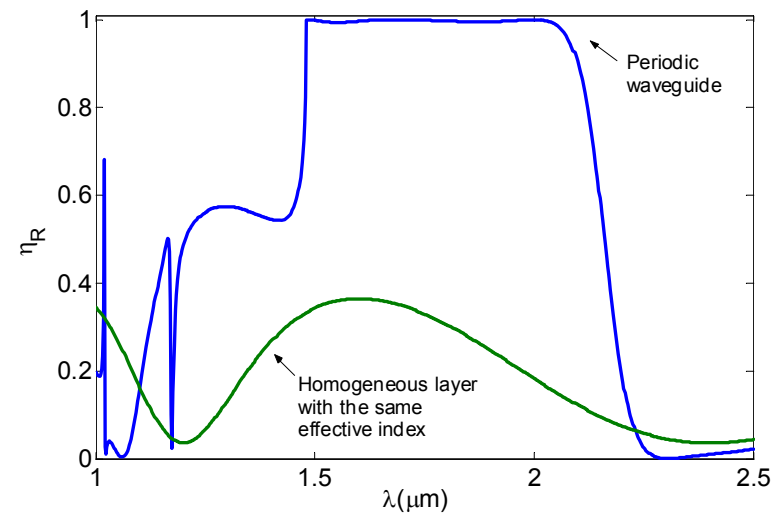
## Weak modulation



- Both edges are lossy
- GMRs appear at both edges
- Resonance separation depends on size of bandgap
- Resonance degeneracy of symmetric case removed

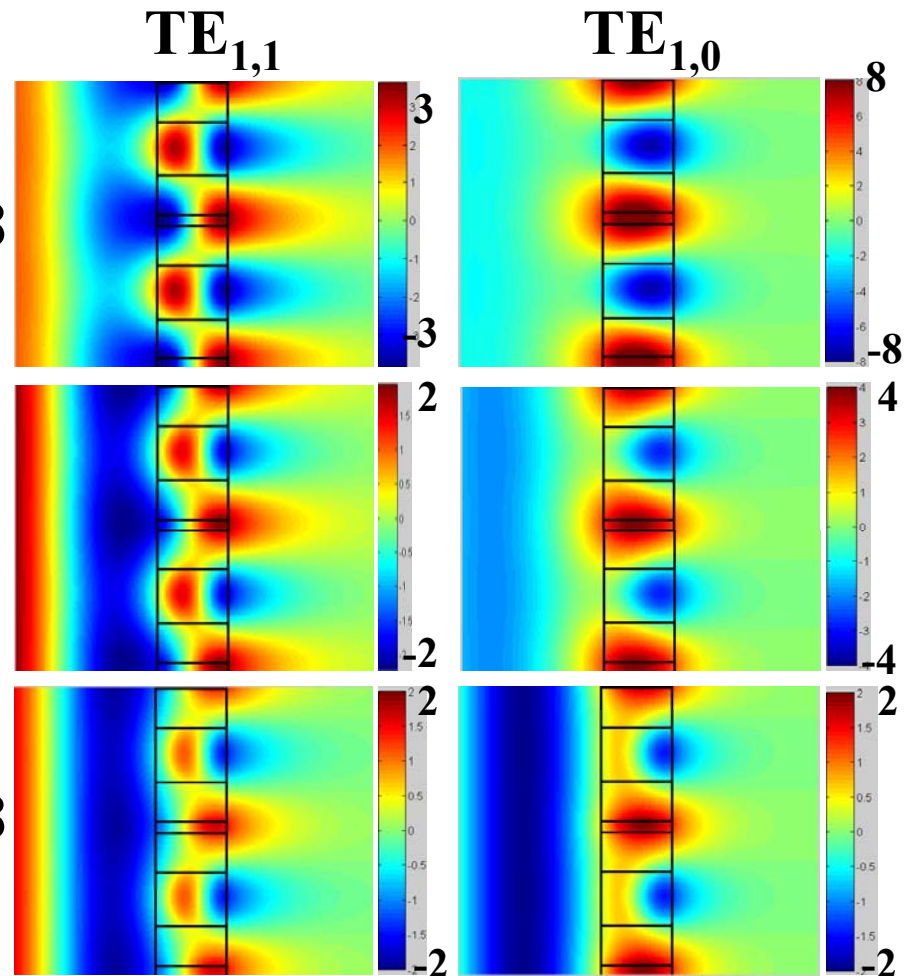
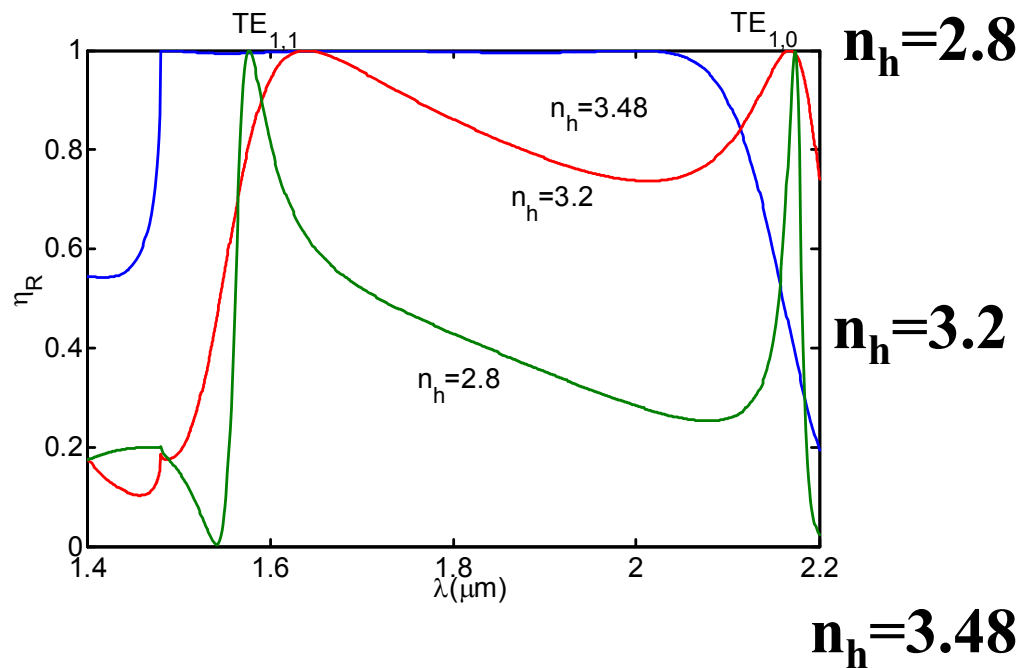
# Resonant SOI leaky-mode reflector

Single layer, TE polarization, 2 resonance peaks



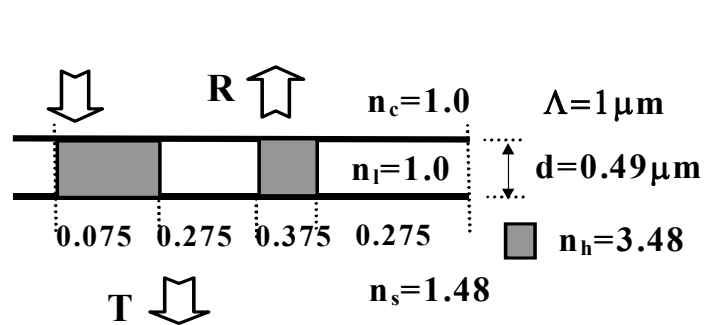
# Resonant leaky-mode reflector: E-fields

Single layer, TE polarization, 2 resonance peaks

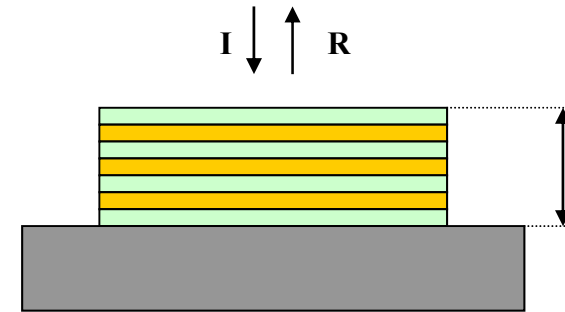
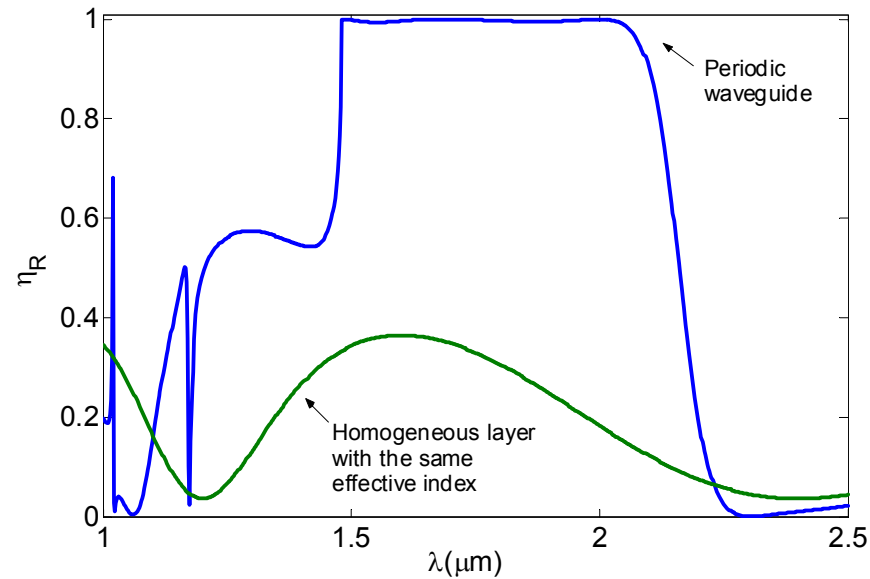




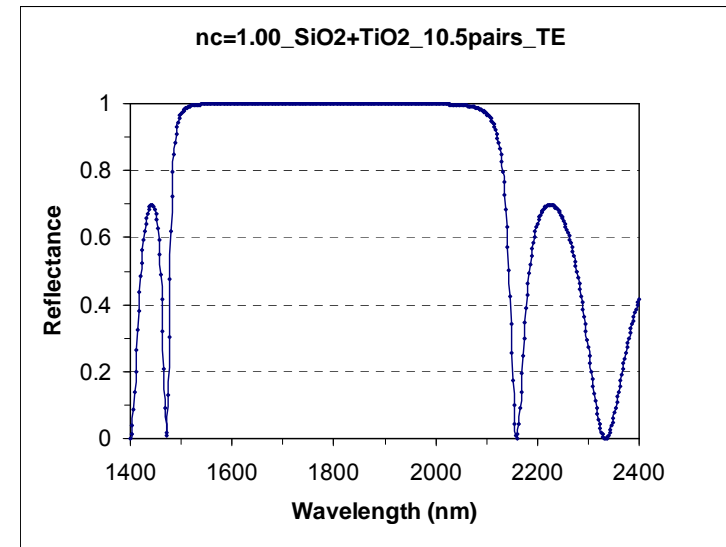
# GMR reflectors vs Bragg stacks



Single-layer SOI resonance device



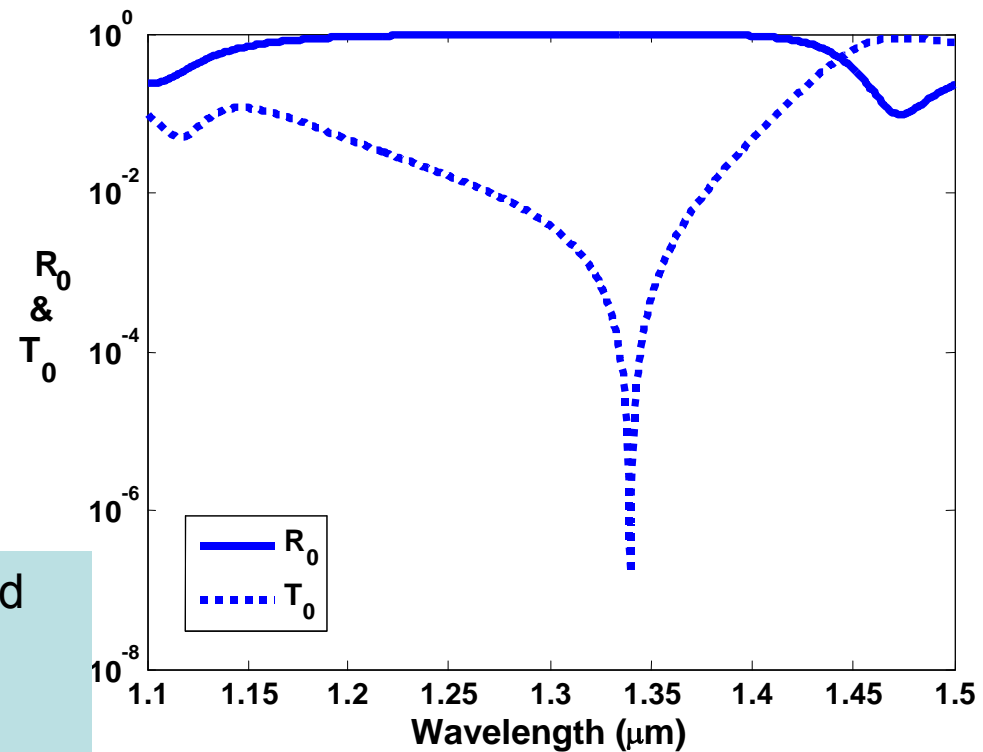
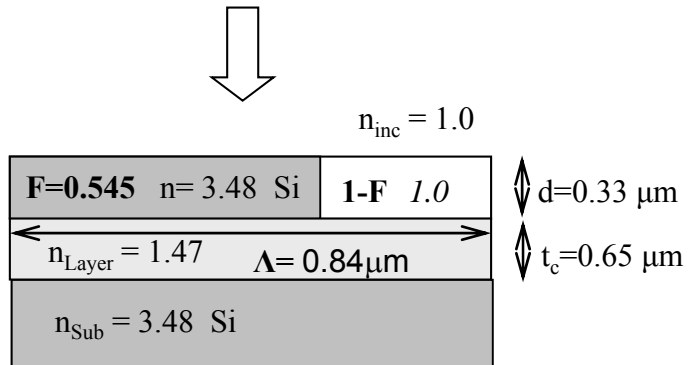
21-layer  $\text{SiO}_2/\text{TiO}_2$  Bragg stack



~600 nm wide reflection band in each case

# Wideband SOI reflector

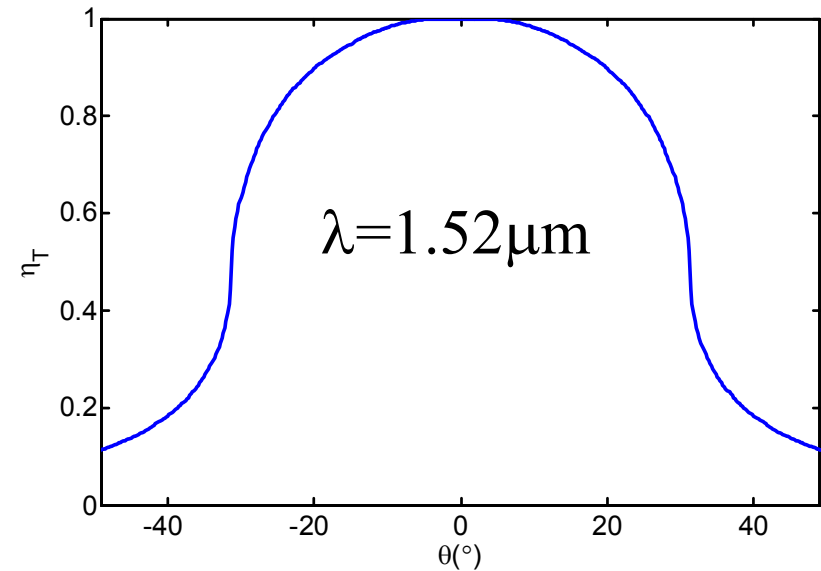
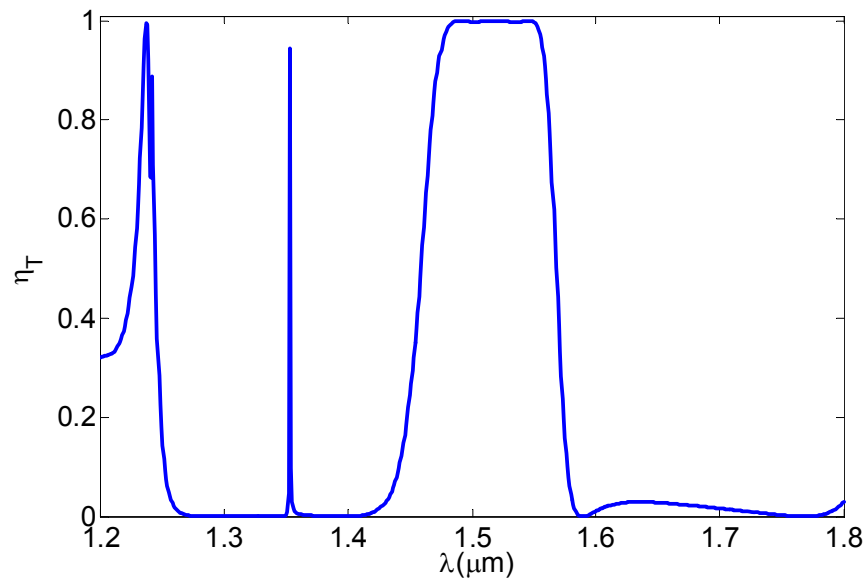
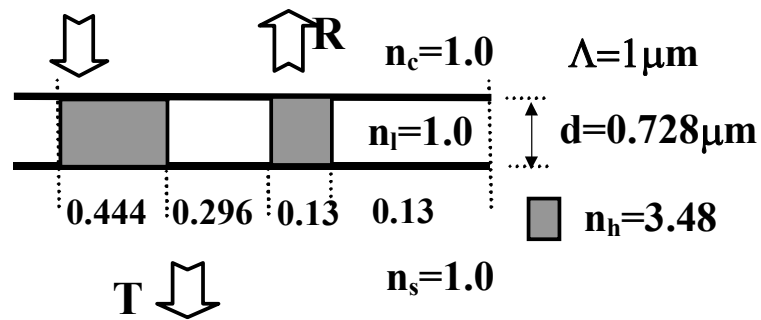
## Single resonance, TE polz



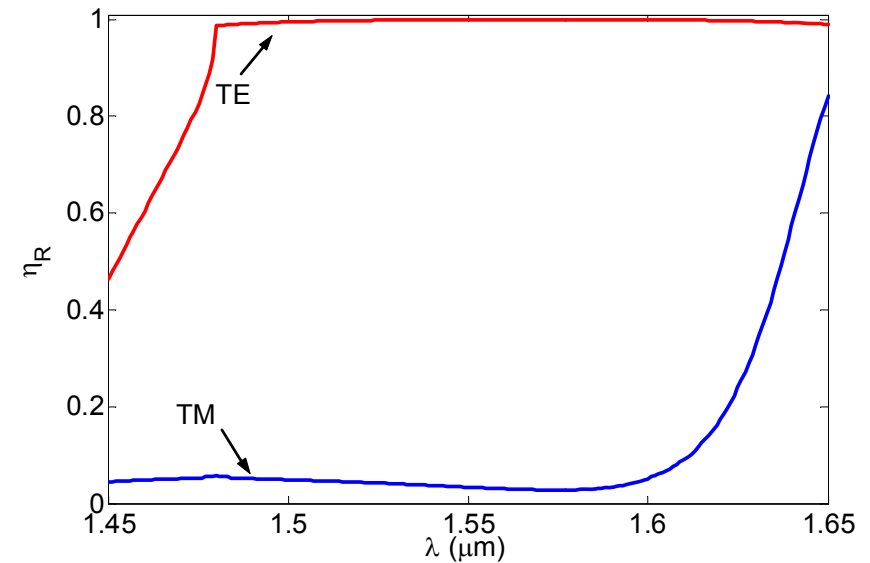
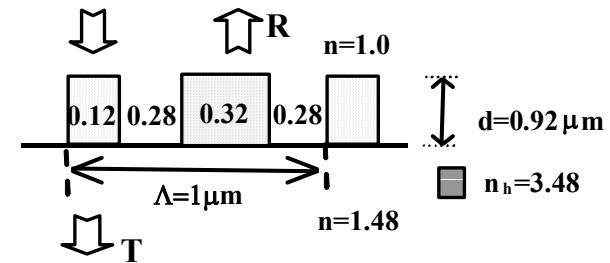
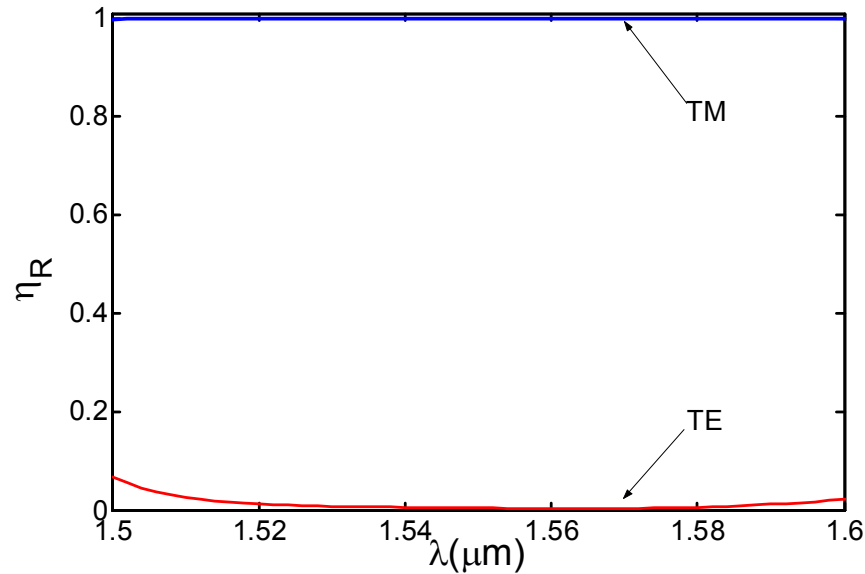
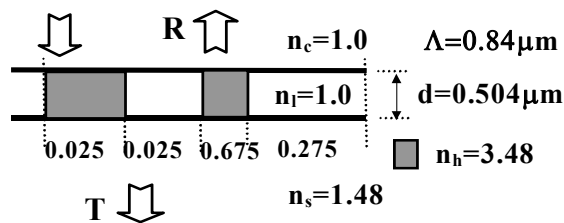
Single-resonance TM-polz wideband reflector experiment reported in:  
Mateus et al, IEEE PTL, July 2004.

# Resonant SOI leaky-mode transmission element

Single layer, TE polarization,  $\sim 100$  nm flattop

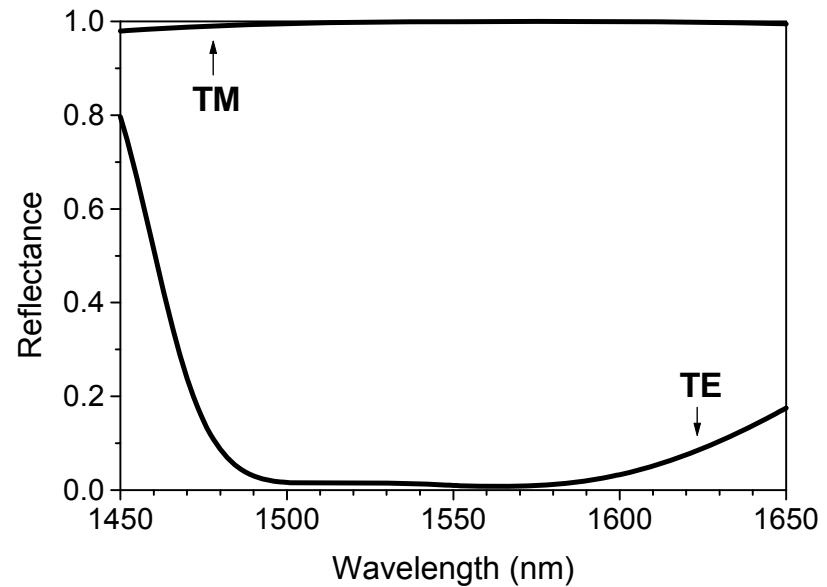
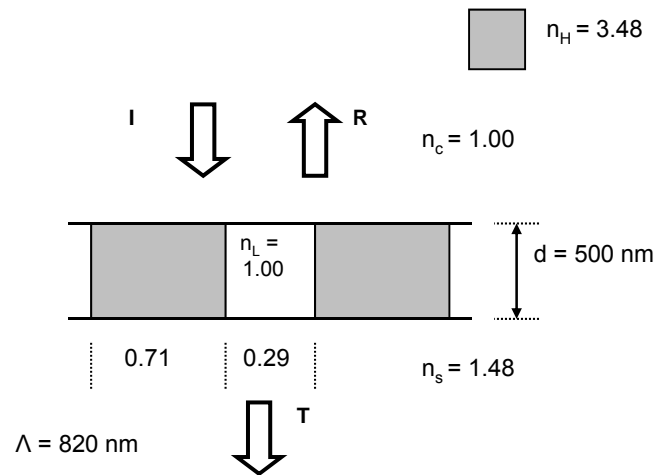


# Resonant SOI leaky mode polarizers



Y. Ding and R. Magnusson, "Resonant leaky-mode spectral-band engineering and device applications," *Optics Express*, vol. 12, 5661-5674 (2004).

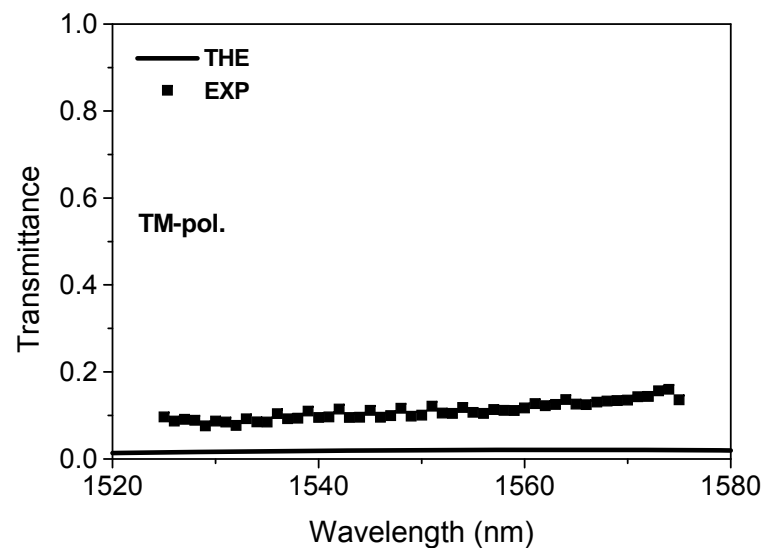
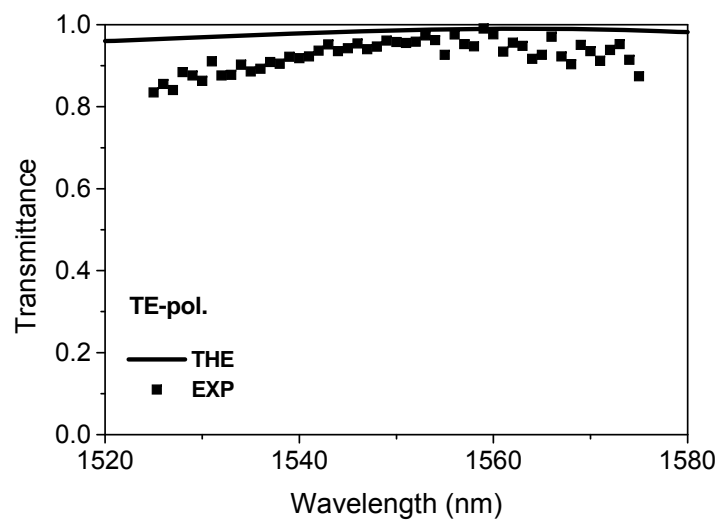
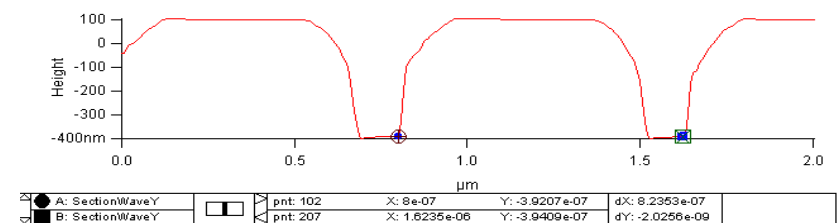
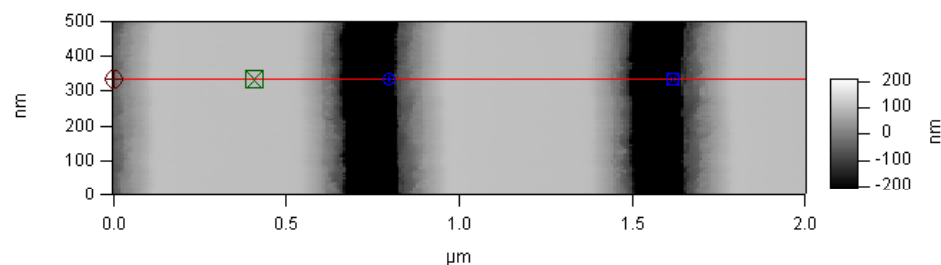
# Fabricated SOI single-layer $\sim 100$ nm polarizer



Goal: Simple fab; higher quality via more complex distribution within period

# AFM image and preliminary polarizer data

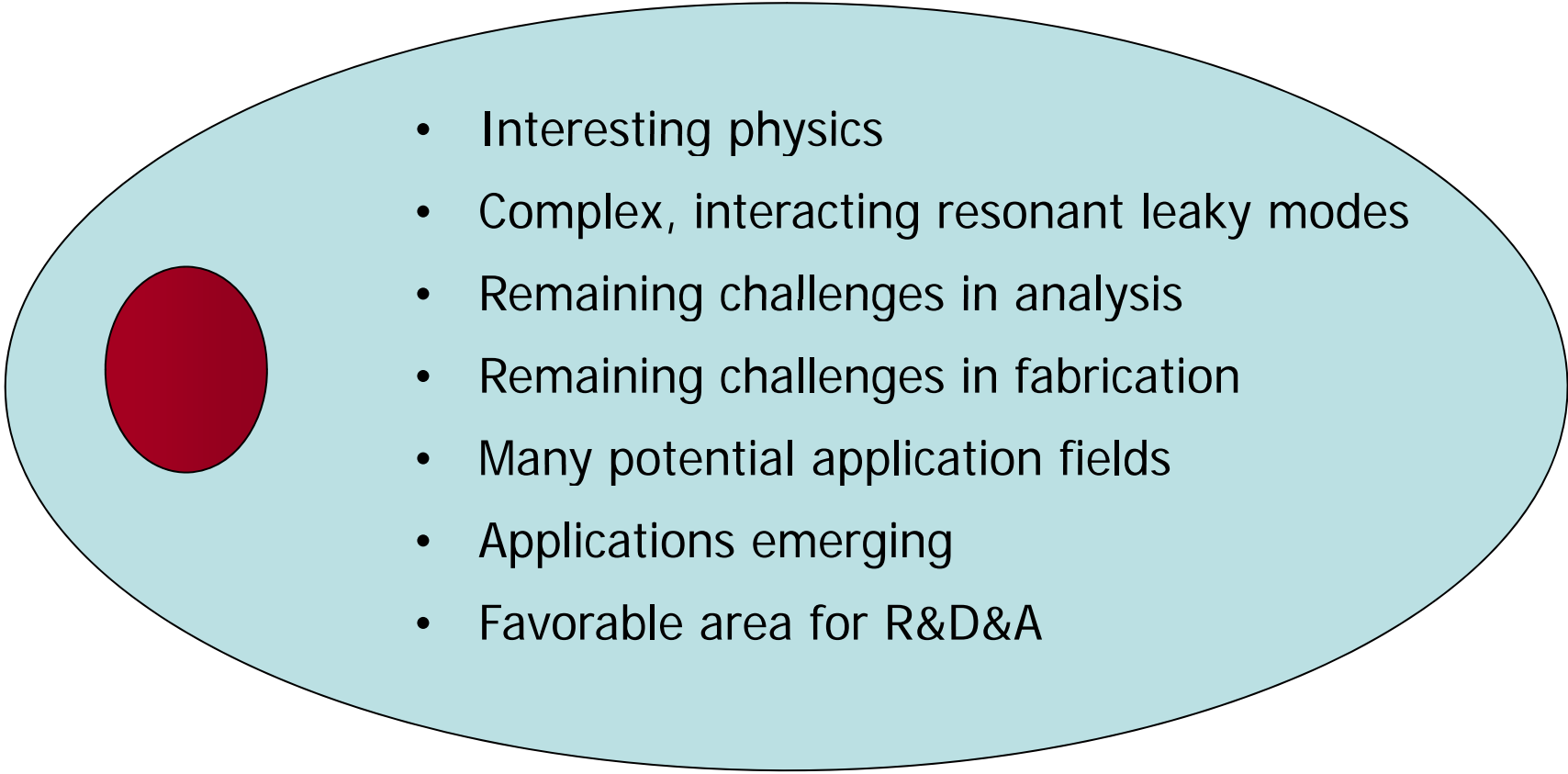
## Electron-beam writing with reactive ion etching



# Leaky-mode resonance technology: Application summary

- Narrow-band reflection (bandstop)/transmission (bandpass) filters ( $\Delta\lambda \sim \text{sub nm}$ )
- Wide-band reflection (bandstop)/transmission (bandpass) filters ( $\Delta\lambda \sim 100\text{'s nm}$ )
- Tunable filters, EO modulators, and switches
- Mirrors for vertical cavity lasers
- Wavelength division multiplexing (WDM)
- Polarization independent elements
- Reflectors
- Polarizers
- Security devices
- Laser resonator frequency selective mirrors
- Non-Brewster polarizing mirrors
- Laser cavity tuning elements
- Spectroscopic biosensors
- Tunable display pixels

# Leaky-mode resonance photonics: An enabling technology platform

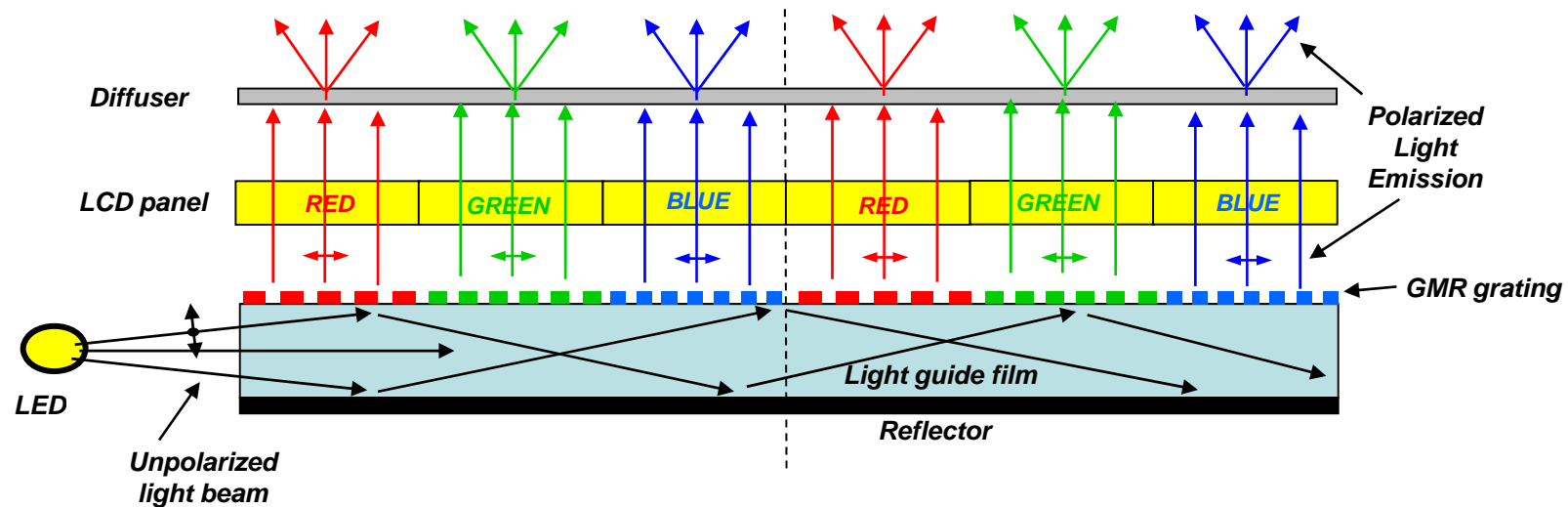
- 
- Interesting physics
  - Complex, interacting resonant leaky modes
  - Remaining challenges in analysis
  - Remaining challenges in fabrication
  - Many potential application fields
  - Applications emerging
  - Favorable area for R&D&A



# In summary

## Key notes

1. What is the GMR effect of waveguide gratings?
2. What is the photonic band structure (or, dispersion relation)?
3. What can we play with GMR filters for display?
4. What are the practical difficulties to be solved in GMR applications?



**Next lecture at 07/07**

- |                |   |
|----------------|---|
| (06/23)        | Introduction: Micro- and nano-optics based on diffraction effect for next generation technologies |
| (06/30)        | Guided-mode resonance (GMR) effect for filtering devices in LCD display panels                    |
| <b>(07/07)</b> | <b>Surface-plasmons: A basic</b>  |
| (07/14)        | Surface-plasmon waveguides for biosensor applications   |
| (07/21)        | Efficient light emission from LED, OLED, and nanolasers by surface-plasmon resonance              |